# Thermodynamics of the Dissociation of Chromium Soap Solutions in Benzene-Dimethyl Formamide

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Critical micelle concentrations and dissociation constants for chromium soaps (myristate, palmitate and stearate) in a mixture of benzene and dimethyl formamide (7:3, vol/vol) were determined by means of conductivity measurements. These soaps behave as simple moderate electrolytes in dilute solutions. Critical micelle concentrations and dissociation constants decreased with increasing numbers of carbon atoms in the soap molecules. Thermodynamic parameters such as heat of dissociation,  $\Delta H_d$ , change in free energy,  $\Delta G_d$ , and entropy,  $\Delta S_d$ , per mole for the dissociation process were also evaluated.

**Key Words:** chromium soaps, conductivity, critical micellar concentration, dissociation constant, thermodynamics.

### Introduction

Metallic soaps are becoming increasingly important in technological uses as well as in academic studies. Application of metallic soaps largely depends on their physicochemical properties such as physical state, thermal stability, chemical reactivity and solubility in polar and non-polar solvents.

Several researchers<sup>1-5</sup> have prepared transition metallic soaps by treating the fatty acid with the requisite amount of metal oxide or hydroxide in the presence of organic solvent or organic base. Physicochemical studies of zinc dicaprylate were described by Mehrotra et al.<sup>6</sup>. The critical micellar concentration (CMC) of nickel, cobalt, manganese, iron, and yttrium soaps at different temperatures were determined conductometrically by Varma et al.<sup>7,8</sup> ad Mehrotra et al.<sup>9,10</sup>.

Mehrotra et al.<sup>11</sup> also determined the density, viscosity, specific viscosity, fluidity, and conductivity of solutions of copper caprylate. In another study Mehrotra et al.<sup>12</sup> investigated the conductance and micellar behavior of praseodymium and neodymium linoleate soaps in a mixture of 60 % benzene and 40 % methanol at different temperatures.

The present paper deals with the evaluation of CMC values, dissociation constants, and the determination of thermodynamic parameters for chromium soaps (myristate, palmitate and stearate) in a mixture of benzene and dimethyl formamide (7:3, vol/vol) by conductivity measurements at different temperatures.

## Experimental

Potassium hydroxide, KOH, chrome alum,  $K_2 SO_4 Cr_2 (SO4)_3$ . 24  $H_2 O$ , myristic acid,  $C_{13}H_{27}COOH$ , palmitic acid,  $C_{15}H_{31}COOH$ , and stearic acid,  $C_{17}H_{35}COOH$ , used in this study were supplied by Merck.

Firstly the potassium soaps were obtained from the reaction between KOH and the fatty acids and then the chromium soaps were prepared by a reaction of potassium soap with the stoichiometrically required amount of chrome alum in a water-alcohol medium (1:1). The precipitated soaps were washed with water and acetone to remove the excess metal ions and unreacted fatty acids and were then dried.

The solutions of soaps were prepared by dissolving a known amount of soap in a benzene-dimethyl formamide mixture (7:3, vol/vol) and were kept for 2 hr in a thermostat at the desired constant temperature.

The reason for the choice of a benzene-dimethyl formamide (7:3, vol/vol) can be explained as follows. A chromium soap (myristate, palmitate and stearate) molecule consists of two parts as a nonpolar saturated hydrocarbon chain and a polar carboxilate end. The myristate, palmitate and stearate salts are very slightly soluble in pure benzene and dimethyl formamide  $^{13}$ . Since benzene is a nonpolar solvent and dimethyl formamide is a polar solvent, the hydrocarbon chain has a tendency to dissolve in benzene and the carboxilate end in dimethyl formamide.

According to the effect of the solvent, the benzene and dimethyl formamide molecules may solvate a chromium soap molecule (for example chromium myristate) as shown in Scheme 1:



Scheme 1.

The hydrocarbon chain is longer and bulkier than the carboxilate end. However, the hydrocarbon chain requires more benzene to dissolve as 7 vol, and dimethyl formamide for the carboxilate end as 3 vol. As a result, the chromium soap molecule dissolves more in a benzene-dimethyl formamide mixture (7:3, vol/vol) than in the pure solvents <sup>14</sup>. For this reason, it seems that this solvent mixture was suitable for our experiments.

The conductance of the soap solutions was measured with an Orion digital conductivity meter, Model 126 (Orion Research Inc., Boston, USA), and a dipping type conductivity cell (cell constant 1.01) with platinized electrodes at different temperatures. The reproducibility of the measurements was  $\pm 0.1\%$ .

**Table 1.** Specific conductance,  $\mathbf{K}/(\text{mhos cm}^{-1})$ , and molar conductance,  $\Lambda/(\text{mhos cm}^2 \text{ mol}^{-1})$  of chromium soaps in a benzene-dimethyl formadide mixture (7:3, vol/vol) at 30°C.

$C \times 10^{3}/$	Myristate		Palmitate		Stearate	
$(mol L^{-1})$	$K \times 10^{6}$	Λ	$K \times 10^{6}$	Λ	$K \times 10^{6}$	Λ
2	1.95	0.975	1.44	0.720	1.19	0.595
3	2.27	0.757	1.67	0.557	1.39	0.463
4	2.60	0.650	1.89	0.473	1.58	0.395
5	2.92	0.584	2.11	0.422	1.78	0.356
6	3.24	0.540	2.35	0.392	2.01	0.335
7	3.59	0.513	2.65	0.379	2.26	0.323
8	3.96	0.495	2.94	0.368	2.51	0.314
9	4.32	0.480	3.25	0.361	2.75	0.306
10	4.68	0.468	3.54	0.354	3.00	0.300

**Table 2.** Critical micellar concentrations of chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol) at various temperatures.

	$CMC \times 10^3 / \pmod{L^{-1}}$					
Soap	$30^{\circ}\mathrm{C}$	$40^{\circ}\mathrm{C}$	$50^{\circ}\mathrm{C}$	$60^{\circ}\mathrm{C}$		
Chromium myristate	6.2	6.7	7.0	7.3		
Chromium palmitate	5.8	6.2	6.5	6.8		
Chromium stearate	5.4	5.8	6.1	6.4		

#### **Results and Discussion**

Specific conductance,  $\mathbf{K}$ , of the solutions of chromium soaps (myristate, palmitate, and stearate) in a mixture of benzene and dimethyl formamide (7:3, vol/vol) increased with increasing soap concentration and decreasing numbers of carbon atoms in the soap (Table 1).

Molar conductance,  $\Lambda$ , of the chromium soap solutions in a benzene-dimethyl formamide (7:3, vol/vol) mixture decreased with increasing concentration and chainlength of the soap (Table 1). The decrease in molar conductance is attributed to the combined effects of ionic atmosphere, solvation of ions, and decrease of mobility and ionization with the formation of micelles.

The increase in specific conductance with soap concentration may have been due to dissociation of chromium soaps into simple chromium metal cations  $(Cr^{3+})$  and fatty acid anions  $(RCOO^{-})$ , where R is  $C_{13}H_{27}$ ,  $C_{15}H_{31}$ , and  $C_{17}H_{35}$  for myristate, palmitate, and stearate, respectively, in dilute solutions and due to the formation of micelles at higher soap concentrations (C > 0.005 M)

The decrease in specific conductance with increasing number of carbon atoms in the fatty acid chain of the soap molecules may have been due to the higher molecular weight and decreasing mobility of anions. Plots of specific conductance,  $\mathbf{K}$ , vs. soap concentration,  $\mathbf{C}$ , (Figures 1 and 2) are characterized by a break, corresponding to **CMC** (Table 2), which shows that micelle formation takes place at a definite soap concentration.







Since the molar conductance of the solutions of chromium soaps does not vary linearly with the square root of soap concentration, the Debye-Hückel-Onsager equation <sup>15</sup> is not applicable to these solutions. Molar conductance results show that chromium soaps behave as weak electrolytes in solution. Ionization of chromium soaps may be explained by Ostwald's formula.

If C is the concentration and  $\alpha$  is the degree of dissociation of the chromium soap, molar concentration may be represented as follows:

$$Cr(RCOO)_3 \rightleftharpoons Cr^{3+} + 3RCOO^-$$

$$C(1-\alpha)$$
  $C\alpha$   $3C\alpha$ 

The dissociation cnostant,  $\mathbf{K}_d,$  for this equilibrium may be expressed as follows:

$$K_d = \frac{\left[Cr^{3+}\right] \left[RCOO^{-}\right]^3}{\left[Cr(RCOO)_3\right]} = \frac{27C^3\alpha^4}{(1-\alpha)} \tag{1}$$

Since ionic concentrations are low and interionic effects are almost negligible in dilute solutions, the solutions of soaps do not deviate appreciably from ideal behavior, and the activities of ions can be taken as almost equal to the concentrations. The degree of dissociation,  $\alpha$ , may be replaced by the conductance ratio,

 $\Lambda/\Lambda_{\infty}$ , where  $\Lambda$  is molar conductance at finite concentration and  $\Lambda_{\infty}$  is the limiting molar conductance at infinite dilution.

By substituting the value of  $\alpha$  and rearranging, Equation 1 can be rewritten as follows:



Figure 2. Specific conductance vs. concentration plots o chromium myristate in a benzene-dimethyl formamide mixture (7:3, vol/vol) at various temperatures. 0:  $30^{\circ}$  C,  $\Box$ :  $40^{\circ}$  C,  $\Delta$ :  $50^{\circ}$  C and  $\diamond$ :  $60^{\circ}$  C.

The values of  $\mathbf{K}_d$  (Table 4) were calculated from the slope  $[(\mathbf{K}_d \Lambda_{\infty}^4) \mathbf{27}]$  and intercept  $[-(\mathbf{K}_d \Lambda_{\infty}^3)/\mathbf{27}]$  of the linear portion of the plots of  $\Lambda^3 \mathbf{C}^3$  vs.  $\mathbf{1}/\Lambda$  below the CMC (Table 3 and Figure 3). It is seen that the values of  $\mathbf{K}_d$  decreased with an increase in the numbers of carbon atoms in the soap molecules, i.e., with increasing chainlength of the soap.

However, the decrease in the values of dissociation constant with increasing temperature indicates the exothermic nature of the dissociation of chromium soaps (myristate, palmitate and stearate) in a benzenedimethyl formamide mixture (7:3, vol/vol).

The heat of dissociation,  $\Delta \mathbf{H}_d$ , for chromium soaps (myristate, palmitate and stearate) is determined with the following equation<sup>12</sup>:

$$\frac{\partial(\log K_d)}{\partial T} = \frac{\Delta H_d}{RT^2} \tag{3}$$

or

$$logK_d = -\frac{\Delta H_d}{2.303RT} + C \tag{4}$$

The values of heat of dissociation,  $\Delta \mathbf{H}_d$ , were obtained from the slope of the linear plots of  $\log \mathbf{K}_d$  vs.  $1/\mathbf{T}$  (Figure 4), and are shown in Table 5. The negative values of heat of dissociation,  $\Delta \mathbf{H}_d$ , indicate that the dissociation process for chromium soaps is exothermic in nature.

**Table 3.** The values of  $\Lambda^3 \mathbf{C}^3$  and  $1/\Lambda$  for chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol) at 30 ° C.

Myristate		Palmita	te	Stearate		
$\Lambda^3 \mathrm{C}^3 \times 10^{16}$	$1/\Lambda$	$\Lambda^3 \mathrm{C}^3 \times 10^{16}$	$1/\Lambda$	$\Lambda^3 \mathrm{C}^3 \times 10^{16}$	$1/\Lambda$	
0.0742	1.0256	0.0299	1.3889	0.0169	1.6807	
0.1170	1.3210	0.0466	1.7953	0.0269	2.1598	
0.1758	1.5385	0.0675	2.1142	0.0394	2.5317	
0.2490	1.7123	0.0939	2.3697	0.0564	2.8090	
0.3401	1.8519	0.1298	2.5510	0.0812	2.9851	
0.4627	1.9493	0.1861	2.6385	0.1154	3.0960	
0.6210	2.0202	0.2541	2.7174	0.1581	3.1847	
0.8062	2.0833	0.3433	2.7700	0.2080	3.2680	
1.0250	2.1368	0.4436	2.8249	0.2700	3.3333	



Figure 3. The plot of  $\Lambda^3 C^3$  vs.  $1/\Lambda$  of chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol) at 303 K. 0: chromium myristate,  $\Box$ : chromium palmitate and  $\Delta$ : chromium stearate.

**Table 4.** Dissociation constants,  $\mathbf{K}_d$  (from the plot of  $\Lambda^3 \mathbf{C}^3$  vs.  $1/\Lambda$ ), of chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol) at various temperatures.



Figure 4. The log  $K_d$  vs.  $1/\Lambda$  of chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol) at 303 K. 0: chromium myristate,  $\Box$ : chromium palmitate and  $\Delta$ : chromium stearate.

The values of change in free energy,  $\Delta \mathbf{G}_d$ , and entropy,  $\Delta \mathbf{S}_d$  per mole for the dissociation process are calculated by using the relationships<sup>12</sup>:

$$\Delta G_d = -RT ln K_d \tag{5}$$

$$\Delta S_d = \frac{\Delta H_d - \Delta G_d}{T} \tag{6}$$

The calculated values of  $\Delta \mathbf{G}_d$  and  $\Delta \mathbf{S}_d$  are shown in Table 6. Careful scrutiny of the thermodynamic parameters indicates that the positive values of  $\Delta \mathbf{G}_d$  and negative values of  $\Delta \mathbf{S}_d$  for the dissociation process (Table 6) show that the dissociation process is a nonspontaneous occurance physicochemically for chromium soaps (myristate, palmitate and stearate) in a benzene-formamide mixture (7:3, vol/vol).

**Table 5.** The values of heat of dissociation,  $\Delta \mathbf{H}_d$ , of chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol).

	Heat of dissociation
Soap	$\Delta { m H}_d/~{ m kJ}~{ m mol}^{-1}$
Chromium myristate	-22.82
Chromium palmitate	-40.20
Chromium stearate	-44.00

**Table 6.** The values of change in free energy,  $\Delta \mathbf{G}_d$ , and entropy,  $\Delta \mathbf{S}_d$ , per mole for the dissociation process of chromium soaps in a benzene-dimethyl formamide mixture (7:3, vol/vol) at various temperatures.

	$\Delta~{ m G}_d/~{ m kJ}~{ m mol}^{-1}$			$\Delta \mathrm{S}_d \times 10^2 / \mathrm{K}^{-1} \mathrm{mol}^{-1}$				
Soap	$30^{\circ}\mathrm{C}$	$40^{\circ}\mathrm{C}$	$50^{\circ}\mathrm{C}$	$60^{\circ}\mathrm{C}$	$30^{\circ}\mathrm{C}$	$40^{\circ}\mathrm{C}$	$50^{\circ}\mathrm{C}$	$60^{\circ}\mathrm{C}$
Chromium myristate	36.59	38.55	40.68	42.50	-19.61	-19.61	-19.66	-19.59
Chromium palmitate	36.92	39.66	42.20	44.55	-25.45	-25.51	-25.51	-25.45
Chromium stearate	38.46	40.75	43.61	46.58	-27.22	-27.08	-27.12	-27.20

However, as can be seen in Table 6, the values of change in free energy,  $\Delta \mathbf{G}_d$ , increased with increasing temperature whereas the values of entropy,  $\Delta \mathbf{S}_d$ , decreased. Since the solute ions are aggregated to form the colloidal particules as micelles near the CMC value and after the CMC the micellization process is replaced the dissociation process, the negative changes of entropy may be obtained below the CMC value.

According to our previous work<sup>16</sup>, the parameters for the thermodynamics of dissociation and micellization of sodium, calcium, aluminum and tin stearates in mixed organic solvents indicates that the negative values of  $\Delta \mathbf{G}_m$  and positive values of  $\Delta \mathbf{S}_m$  for the micellization process and positive values of  $\Delta \mathbf{G}_d$  and negative values of  $\Delta \mathbf{S}_d$  for the dissociation process show that the micellization process is favored over the dissociation process and the micellization is a spontaneous occurance but the dissociation is nonspontaneous.

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