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**Research Article** 

# Induction motor parameter estimation using metaheuristic methods

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Abstract: The steady-state equivalent circuit parameters of an induction motor can be estimated using the operation characteristics that are provided by manufacturers. The characteristics of the motor used in estimation methods are the starting, maximum, and nominal torque values; the power factor; and efficiency. The operation characteristics of a motor given in data sheets are generally based on design parameters and are not suitable with real values. For this reason, in this paper, the data used in the parameter estimation for induction motors are taken from the literature. Using an optimization method for parameter estimation is useful for comparing the manufacturer values and values at the end of estimation, as well as minimizing the error in between. There are many methods in the literature for the parameter estimation of induction motors. In this study, the estimation is made using the charged system search (CSS), differential evolution algorithm (DEA), particle swarm optimization, and genetic algorithm optimization techniques. The CSS algorithm is first applied for estimation of the parameters of an induction motor. The results obtained from all of the methods show that the CSS algorithm is suitable with the DEA. From the obtained results, it is understood that an exact approach can be made to equivalent circuit parameters in case the values given by the manufacturer model the motor properly.

**Key words:** Induction motor, exact equivalent circuit parameters, torque values, charged system search, differential evolution algorithm, particle swarm optimization, genetic algorithm

## 1. Introduction

Induction motors have important problems, such as transient and quasi-steady-state stability. To solve the steady-state stability problems of an induction motor, equivalent circuit parameters are required. These parameters are the resistances and reactances of the stator and rotor, including magnetizing branches. Estimation of these parameters is particularly essential in determining their effects on motor performance. The main difficulty in constructing an accurate motor model is the unavailability of manufacturer data for estimation. Hence, explicit representation of induction motor models is not given in various applications. In the conventional techniques, estimation of the induction motor parameters is based on no-load and blocked-rotor tests [1].

Aside from the conventional technique, there are 2 different approaches for parameter estimation, which are online and offline techniques. The former uses the Kalman filter [2] and least square techniques [3]. The latter is offline [4] curve generation for the experimentally measured data. Recently, artificial neural networks

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and various evolutionary algorithms were used with both online and offline methods. In the literature, Wishart and Harley [5] experimented with a method that uses artificial neural networks for induction motor parameter estimation in current and speed control [6]. Linear techniques based on dynamic model and neuro-fuzzy methods are also proposed for the estimation of induction motor parameters [7,8]. In [9–11], the estimation of the stator resistance, transient inductance, and rotor resistance online were discussed. An interesting approach for tuning the rotor resistance was proposed in [12] based on model reference adaptive system schemes [13]. Since some of the above approaches require a derivative of the function, which is not always available or may be difficult to calculate, deterministic approaches often cannot find optimal solutions [1].

Recently, in solving induction motor parameter estimation problems, some new global optimization techniques, such as the evolutionary algorithm [14], genetic algorithm (GA) [15,16], differential evolution [17], particle swarm optimization (PSO) [18], and colony optimization [19], harmony search (HS) [20] and big bang-big crunch [21], hybrid GA [22], and dynamic encoding algorithm for search [23], were proposed [1]. Moreover, the charged system search (CSS) is the most recent metaheuristic algorithm, which utilizes the Newtonian motion law in additional to electrical physics laws to direct the agents in order to recognize the optimum locations [24].

In this study, the CSS, differential evolution algorithm (DEA), PSO, and GA techniques were applied to estimate induction motor parameters. In the implementation of the techniques, 2 different induction motors, the squirrel-cage rotor and wound-rotor, are used. The 30-kW wound-rotor induction motor parameters are taken from [25] and the 37-kW squirrel-cage induction motor parameters are taken from [6].

In the literature, the CSS algorithm is generally used in civil engineering problems. There is no study where the CSS algorithm was applied for the estimation of induction motor equivalent circuit parameters based on torque values  $(T_{st}, T_{max}, \text{ and } T_n)$ . As a preliminary work, in this study, the CSS algorithm was applied to estimate induction motor parameters.

#### 2. Optimization techniques

## 2.1. Charged system search

Kaveh and Talatahari proposed the CSS algorithm [24,26]. The use of this algorithm is growing and its application is extending to various optimization problems [27–35]. A typical algorithm for the CSS is shown in Figure 1.

The CSS algorithm depends on Coulomb and Gauss laws and movement governing the motion laws of Newtonian mechanics. This algorithm can be considered as a multiagent approach, where each agent is a charged particle (CP). Each CP is assumed as a sphere with radius a and a proper charge density, and can be expressed as follows [30]:

$$q_{i} = \frac{fit(i) - fit_{worst}}{fit_{best} - fit_{worst}}, \ i = 1, 2, 3, ..., N.$$
(1)

Here,  $fit_{best}$  and  $fit_{worst}$  are the best and worst fitness values of all of the particles, fit(i) is the fitness of agent i, and N is the total number of CPs. The initial positions of the CPs in search space are determined randomly and Eq. (2) is used for determination.

$$x_{i,j}^{(o)} = x_{i,\min} + rand_{ij} \cdot (x_{i,\max} - x_{i,\min}), \ i = 1, 2, 3, \dots, N$$
(2)

Here,  $x_{i,j}^{(0)}$ , determines the initial value of variable number *i* for CP number *j*,  $x_{i,min}$  and  $x_{i,max}$  are the minimum and maximum allowed values for variable number *I*, and rand *ij* is a randomly generated number



Figure 1. Flowchart of the CSS [27].

within the interval (0,1). The initial velocities of the CPs are taken as below:

$$v_{i,j}^{(o)} = 0, \ i = 1, 2, 3, ..., N.$$
 (3)

Each CP applies a force on the other CPs according to Coulomb's law. The magnitude of this force is proportional with the distance between the CPs for the CP within the sphere, while it is inversely proportional

with the square of the distance between the particles for a located CP outside of the sphere. These forces may come out as attracting or repelling and can be found with the  $ar_{ij}$  force parameter, defined as below:

$$ar_{ij} = \begin{cases} +1 & k_t < rand_{ij} \\ -1 & k_t > rand_{ij} \end{cases}$$

$$\tag{4}$$

The +1 value in Eq. (4) shows that the force is attracting and the -1 value shows that the force is repelling, and  $k_t$  is the parameter controlling the effect of the force type. Usually, the force coming out as attracting gathers the CPs in a certain area within the search area, while the repelling force tries to distribute the CPs. As a result, the force can be defined as below:

$$\mathbf{F}_{j} = \sum_{i,i\neq j} \left( \frac{q_{i}}{a^{3}} r_{ij} \cdot i_{1} + \frac{q_{i}}{r_{ij}^{2}} \cdot i_{2} \right) \cdot ar_{ij} \cdot p_{ij} \cdot (X_{i} - X_{j}) \quad \left( \begin{array}{c} j = 1, 2, 3, \dots, N\\ i_{1} = 1, i_{2} = 0 \Leftrightarrow r_{ij} < a\\ i_{1} = 0, i_{2} = 1 \Leftrightarrow r_{ij} \geq a \end{array} \right)$$
(5)

Here,  $F_j$  is the force value acting on the *j*th CP and  $r_{ij}$  is the distance between 2 CPs, defined as follows:

$$r_{ij} = \frac{\|X_i - X_j\|}{\|(X_i - X_j)/2 - X_{best}\| + \varepsilon}.$$
(6)

Here,  $X_i$  and  $X_j$  are the positions of CPs *i* and *j*, respectively;  $X_{best}$  is the position of the best current CP; and  $\varepsilon$  is a small positive number taken to prevent singularity.  $p_{ij}$  determines the moving possibility of each CP to the others, as below:

$$p_{ij} = \begin{cases} 1 & \frac{fit(i) - fit_{best}}{fit(j) - fit(i)} > rand \lor fit(i) > fit(j) \\ 0 & else \end{cases}$$
(7)

As a result, the forces coming out and the motion laws determine the new CP positions. At this stage, each CP moves toward its new position under the effect of the forces and its previous velocity, as below:

$$X_{j,new} = rand_{j1}.k_a.\frac{\mathbf{F}_j}{m_j}.\Delta t^2 + rand_{j2}.k_v.\mathbf{V}_{j,old}.\Delta t + X_{j,old},\tag{8}$$

$$\mathbf{V}_{j,new} = \frac{X_{j,new} - X_{j,old}}{\Delta t}.$$
(9)

Here,  $k_a$  is the acceleration coefficient,  $k_v$  is the velocity coefficient controlling the influence of the previous velocity, and  $rand_{j1}$  and  $rand_{j2}$  are 2 random numbers distributed to the sequence uniformly within the interval (0,1). If each CP moves out of the CP search space, its position is corrected by a handling approach based on HS. Moreover, the charged memory is used for recording the best results.

#### 2.2. Differential evolution algorithm

The DEA is a heuristic optimization technique depending on the GA in the means of operation. It was developed by Storn and Price in 1995 [36]. Specifically, in problems where continuous data are in question, it gives efficient results. A new individual is obtained by putting chromosomes into the operators one by one (not operating depending on population). During this operation, mutation and crossover operators are used. If the convenience of the new individual is better than that of the old one, the old individual is conveyed to the next generation [37]. The flowchart of the algorithm is given in Figure 2 [38].



Figure 2. Flowchart of the DEA.

The parameters used in the DEA are population size NP, number of variables (number of genes) D, generation  $(1, 2, 3, \ldots, g_{\text{max}})g$ , crossover rate CR, and scaling factor F [38].

The operation steps of the DEA are creation of the initial population, mutation, crossover, and selection. The conduction of these operations is explained below [39–45].

## 2.2.1. Creation of the initial population

In order to produce new chromosomes in the DEA, 3 chromosomes, with the exception of the corresponding chromosome, are needed. Therefore, the population size should be greater than 3 (NP > 3). The production of the initial population, consisting of NP pieces of chromosomes with D dimensions, is found using Eq. (10).

$$x_{j,i,g=0} = x_j^{(l)} + rand_j[0,1].(x_j^{(u)} - x_j^{(l)})$$
(10)

Here,  $x_{j,i,g}$  is the *j* parameter of the *i* chromosome in the *g* generation, and  $(x_j^{(l)}, x_j^{(u)})$  shows the lower and upper values of the variables.

#### 2.2.2. Mutation

Mutation is making random changes to the chromosome genes. In the DEA, 3 chromosomes that are different from each other and the weighted difference chromosome are selected for mutation  $(r_1, r_2, r_3)$ . The difference

of the first 2 is taken and is multiplied by F. In general, F is valued at between 0 and 2. The weighted difference chromosome and third chromosome are added.

$$n_{j,i,g+1} = x_{j,r_3,g} + F.(x_{j,r_1,g} - x_{j,r_2,g})$$
(11)

Here,  $n_{j,i,g+1}$  is the intermediate chromosome exposed to the g + 1 mutation and crossing, and  $r_{1,2,3} \in \{1, 2, 3, \dots, NP\}$   $r_1 \neq r_2 \neq r_3 \neq i$  are the randomly chosen chromosomes that will be used for new chromosome generation.

## 2.2.3. Crossover

The different chromosomes produced by the mutation and the  $x_{i,g}$  chromosome are used to produce a new chromosome  $(u_{i,g+1})$ . Genes for the trial are selected from different chromosomes with CR possibilities and from the corresponding chromosome with (1 - CR) possibility. The  $j = j_{rand}$  condition is used for guaranteeing at least one gene to be taken from the recently produced chromosome. The randomly selected gene in the  $j = j_{rand}$  point is selected from  $n_{j,i,g+1}$  without taking the CR value into consideration.

$$x_{j,u,g+1} = \left\{ \begin{array}{l} x_{j,n,g+1} \ If \ rand[0,1] \le CR \ or \ j = j_{rand} \\ x_{j,i,g} \ otherwise \end{array} \right\}$$
(12)

### 2.2.4. Fitness function

Using the mutation and crossover, 3 chromosomes are used together with the target chromosome; a new (trial) chromosome is obtained. The chromosome that will be conveyed to the new generation (g = g+1) is determined by looking at the suitability value. The fitness function of the target chromosome is already known. The objection function value of the problem is calculated as a suitability function.

#### 2.2.5. Selection

The highly suitable chromosome is conveyed to the next generation. The cycle continues until  $(g = g_{\text{max}})$  and, when the cycle becomes  $g_{\text{max}}$ , the current best individual is taken as the solution.

$$x_{i,g+1} = \left\{ \begin{array}{c} x_{u,g+1} & If \ f(x_{u,g+1}) \le f(x_{i,g+1}) \\ x_{i,g} & else \end{array} \right\}$$
(13)

#### 2.2.6. Stopping criterion

The aim is continuously acquiring chromosomes with better suitability values and having the optimum value (or getting close). This cycle is continued until  $g = g_{\text{max}}$  and stopping the algorithm depends on the determined maximum iteration number.

The GA and PSO process algorithms, which are used for parameter estimation, were taken, respectively, from [46] and [47], and the parameter estimation of the induction motor was done using the formulas therein.

#### 3. Problem formulation

The actual values of the starting torque  $T_{st}$  (act), maximum torque  $T_{max}$  (act), and nominal torque  $T_n$  (act) are used to estimate the stator resistance and leakage reactance  $(R_1, X_1)$ , rotor resistance and leakage reactance  $(R_2, X_2)$ , and magnetizing reactance  $(X_m)$  parameters. The actual values are the literature values of the motors. The induction motor one-phase exact equivalent circuit model is shown in Figure 3.



Figure 3. One-phase exact equivalent circuit model.

The torque functions  $[T_n(cal), T_{st}(cal), \text{ and } T_{max}(cal)]$  can be written as follows [48]:

$$T_n\left(cal\right) = \frac{KR_2}{s\left[\left(R_{th} + \frac{R_2}{s}\right)^2 + X^2\right]},\tag{14}$$

$$T_{st}(cal) = \frac{KR_2}{(R_{th} + R_2)^2 + X^2},$$
(15)

$$T_{\max}(cal) = \frac{K}{2\left[R_{th} + \sqrt{R_{th}^2 + X^2}\right]}.$$
 (16)

Here,  $T_n$  (cal),  $T_{st}$  (cal), and  $T_{max}$  (cal) stand for the nominal, starting, and maximum torques, respectively, with the following set of equations:

$$K = \frac{3V_{th}^2}{\omega_s}, V_{th} = \frac{X_m}{X_1 + X_m} V_{ph}, R_{th} = \frac{X_m}{X_1 + X_m} R_1, X_{th} = \frac{X_m}{X_1 + X_m} X_1, X = X_2 + X_{th}.$$
 (17)

Here,  $V_{th}$ ,  $R_{th}$ , and  $X_{th}$  are the Thevenin voltage, resistance, and reactance, respectively. K is the constant coefficient,  $\omega_s$  is the angular velocity, s is the slip, and  $V_{ph}$  is the supply voltage. The fitness value of each of the motor torque equations is given in Eq. (18).

$$E_{1} = \left| \frac{T_{n}(act) - T_{n}(cal)}{T_{n}(act)} \right|$$

$$E_{2} = \left| \frac{T_{st}(act) - T_{st}(cal)}{T_{st}(act)} \right|$$

$$E_{3} = \left| \frac{T_{\max}(act) - T_{\max}(cal)}{T_{\max}(act)} \right|$$
(18)

Here,  $E_1$ ,  $E_2$ , and  $E_3$  show the error in the nominal torque, error in the starting torque, and error in the maximum torque, respectively. The total error  $(E_T)$  is given in Eq. (19).

$$E_T = |E_1 + E_2 + E_3| \tag{19}$$

The specifications of the motors used in the modeling are given in Table 1.

Specifications	Motor 1	Motor 2
Nominal power (kW)	30	37
Nominal voltage (V)	460	460
Nominal frequency (Hz)	60	60
Number of poles	4	4
Nominal speed (rpm)	1740	1705
Cage type	Wound-rotor	Squirrel-cage

Table 1.	Specifications	of the	motors
Table T	opeometriono	01 0110	111000010

In all of the methods, at the beginning of the estimation process, the equivalent circuit parameter values are assigned randomly. Error values are checked at every iteration and the minimum error values are obtained by keeping the best parameter values. The equivalent circuit parameters of the 2 motors obtained with the 4 methods and actual values of these parameters are given in Table 2. The actual torque values and calculated torque values are shown in Table 3.

**Table 2.** Comparison of CSS, DEA, PSO, and GA equivalent circuit parameter results with the actual values for motors1 and 2.

$\operatorname{CSS}$					
Motor 1			Motor 2		
Actual values	Estimation values	Error (%)	Actual values	Estimation values	Error (%)
0.25	0.2449278895	2.028844	0.087	0.082946564751	4.659120
0.2	0.1894845257	5.257737	0.228	0.221580835077	2.815423
1	0.9532414585	4.675854	0.604	0.606414293453	0.399717
30	9.1881489419	69.372836	13.08	13.730553467747	4.973650
DEA					
Motor 1			Motor 2		
Actual values	Estimation values	Error (%)	Actual values	Estimation values	Error (%)
0.25	0.2486516245	0.539350	0.087	0.0835084377	4.013289
0.2	0.1952899383	2.355030	0.228	0.2241465675	1.690101
1	0.9866666553	1.333334	0.604	0.6070739183	0.508926
30	33.888837422	12.962791	13.08	13.0812247645	0.009363
PSO					
Motor 1			Motor 2		
Actual values	Estimation values	Error (%)	Actual values	Estimation values	Error (%)
0.25	0.2451853615	1.9258554	0.087	0.0839569063	3.497808
0.2	0.1898968813	5.05155935	0.228	0.2264489983	0.680263
1	0.9570055972	4.29944028	0.604	0.6092982790	0.877198
30	10.9932328108	63.35589063	13.08	13.1422295778	0.475761
GA					
Motor 1			Motor 2		
Actual	Estimation values	E (07)	Actual	Estimation values	E
values	Estimation values		values	Estimation values	
0.25	0.253165663877	1.26626555	0.087	0.0861628266	0.962268
0.2	0.202805246167	1.40262308	0.228	0.2375407538	4.184541
1	1.00624377900	0.62437790	0.604	0.6296539100	4.247336
30	14.749359845505	50.83546718	13.08	15.0626354814	15.15776
	CSS Motor 1 Actual values 0.25 0.2 1 30 DEA Motor 1 Actual values 0.25 0.2 1 30 PSO Motor 1 Actual values 0.25 0.2 1 30 CS 0.2 1 30 GA Motor 1 Actual values 0.25 0.2 1 30 GA Motor 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0.2 1 30 CS 0 1 30 CS 0 1 30 CS 1 30 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 CS 1 30 30 30 30 30 30 30 30 30 30 30 30 30	CSS         Motor 1         Actual values       Estimation values         0.25       0.2449278895         0.2       0.1894845257         1       0.9532414585         30       9.1881489419         DEA       Motor 1         Actual values       Estimation values         0.25       0.2486516245         0.2       0.1952899383         1       0.9866666553         30       33.888837422         PSO       0.2451853615         Motor 1       Estimation values         Actual values       Estimation values         0.25       0.2451853615         0.2       0.19597055972         30       10.9932328108         GA       Estimation values         GA       0.25         Motor 1       0.0250702         30       10.9932328108         GA       Estimation values         0.25       0.253165663877         0.2       0.202805246167         1       1.00624377900         30       14.749359845505	CSSMotor 1Actual valuesEstimation valuesError (%) $0.25$ $0.2449278895$ $2.028844$ $0.2$ $0.1894845257$ $5.257737$ $1$ $0.9532414585$ $4.675854$ $30$ $9.1881489419$ $69.372836$ DEA $V$ $V$ Motor 1 $Actual$ valuesEstimation values $0.25$ $0.2486516245$ $0.539350$ $0.25$ $0.2486516245$ $0.539350$ $0.2$ $0.1952899383$ $2.355030$ $1$ $0.9866666553$ $1.333334$ $30$ $33.888837422$ $12.962791$ PSO $V$ $V$ Motor 1 $Actual$ valuesEstimation values $Actual$ valuesEstimation valuesError (%) $0.25$ $0.2451853615$ $1.9258554$ $0.2$ $0.1898968813$ $5.05155935$ $1$ $0.9570055972$ $4.29944028$ $30$ $10.9932328108$ $63.35589063$ $GA$ $V$ $V$ Motor 1 $Actual$ valuesError (%) $0.25$ $0.253165663877$ $1.26626555$ $0.2$ $0.202805246167$ $1.40262308$ $1$ $1.00624377900$ $0.62437790$ $30$ $14.749359845505$ $50.83546718$	$\begin{array}{ c c c c c c } CSS & & & & & & & & & & & & & & & & & &$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $

	CSS							
	Motor 1			Motor 2	Motor 2			
Demomentary	Actual	Estimation values	$\mathbf{E}_{max}\left( 0^{\prime}\right)$	Actual	Estimation values	$\mathbf{E}_{mon}\left( 0^{\prime}\right)$		
rarameters	values	Estimation values	E1101 (70)	values	Estimation values 529.7080887509 773.9868719304 234.5501880796 Estimation values 529.7079528896 773.9869326887 234.5497933898 Estimation values 529.7043502484 773.9652578505 234.5535738994 Estimation values 529.7145521087 773.9774822166	E1101 (70)		
$T_{st}$	163.11	163.1099999558	2.708356e-8	529.708	529.7080887509	1.675470e-5		
$T_{\rm max}$	431.68	431.6800000193	4.486425e-9	773.987	773.9868719304	1.654673e-5		
$T_n$	185.20	185.1999999592	2.198434e-8	234.55	234.5501880796	8.018743e-5		
	DEA	-						
	Motor 1			Motor 2				
Demonstern	Actual	<b>T</b> -4:	$\mathbf{E}_{max}(07)$	Actual	<b>D</b> -t:t:l	$\mathbf{E}_{max}(07)$		
Parameters	values	Estimation values	Error (%)	values	Estimation values 529.7080887509 773.9868719304 234.5501880796 2 Estimation values 529.7079528896 773.9869326887 234.5497933898 2 Estimation values 529.7043502484 773.9652578505 234.5535738994 2 Estimation values 529.7145521087 773.9774822166 234.5654525646	Error $(\%)$		
$T_{st}$	163.11	163.1099999996	2.452332e-10	529.708	529.7079528896	8.893638e-6		
$T_{\rm max}$	431.68	431.6800000121	2.803928e-11	773.987	773.9869326887	8.696692e-6		
$T_n$	185.20	185.2000000001	8.153347e-11	234.55	234.5497933898	8.808789e-5		
	PSO							
	Motor 1			Motor 2				
Deverators	Actual	Estimation values	$\mathbf{F}_{\mathbf{rror}}(\mathbf{\mathcal{O}})$	Actual	Estimation values	$\mathbf{F}_{\mathbf{rror}}(\mathbf{\mathcal{O}})$		
1 arameters	values	Estimation values	E1101 (70)	values	$\begin{array}{c c} \text{ or } 2 \\ \hline \text{ial} \\ \text{es} \\ \hline \text{Estimation values} \\ \hline 708 \\ 529.7079528896 \\ \hline 987 \\ 773.9869326887 \\ \hline 55 \\ 234.5497933898 \\ \hline \text{or } 2 \\ \hline \text{ial} \\ \text{es} \\ \hline \text{Estimation values} \\ \hline 708 \\ 529.7043502484 \\ \hline 987 \\ 773.9652578505 \\ \hline 55 \\ 234.5535738994 \\ \hline \end{array}$	E1101 (70)		
$T_{st}$	163.11	163.1065040937	2.143281e-3	529.708	529.7043502484	6.890119e-4		
$T_{\rm max}$	431.68	431.6801038641	2.406043e-5	773.987	773.9652578505	2.809110e-3		
$T_n$	185.20	185.2026973711	1.456463e-3	234.55	234.5535738994	1.523726e-3		
	GA							
	Motor 1			Motor 2				
Demomentaria	Actual	Estimation values	$\mathbf{F}_{mon}(0^{\prime})$	Actual	Estimation values	$\mathbf{E}_{max} \left( 07 \right)$		
rarameters	values	Estimation values	E1101 (70)	values	Estimation values	E1101 (70)		
$T_{st}$	163.11	163.089203340828	12.75008e-3	529.708	529.7145521087	1.236928e-3		
$T_{\rm max}$	431.68	431.690235169530	2.371008e-3	773.987	773.9774822166	1.229708e-3		
$T_n$	185.20	185.191088011981	4.812088e-3	234.55	234.5654525646	6.588175e-3		

Table 3. Comparison of CSS, DEA, PSO, and GA torque results with the actual values for motors 1 and 2.

When the results obtained for both motors are examined, it is seen that the error values of the equivalent circuit parameters are at acceptable levels. Here, compared with the other parameters, the error values of the  $X_m$  parameter are greater. However, the  $X_m$  value has no direct effect on the torque formulation. Thus, the error values of the  $X_m$  parameter can be ignored.

When examined in terms of the torque calculation, it is seen that the DEA obtains the best result. The torque values obtained by the CSS are close to those of the DEA. The biggest error values are obtained from the GA method.

The change of fitness values according to the iteration is shown in Figures 4 and 5 for motors 1 and 2, respectively.

When Figure 4 is examined, it is seen that the DEA method converges at the smallest iteration number. After the DEA, the CSS algorithm has the best convergence value for motor 1. It is seen that the PSO algorithm converges at the 125th iteration. However, it is seen that the GA is not able to reach the convergence values.

When Figure 5 is examined, it is seen that the DEA again has the best convergence. It is seen that the CSS algorithm similarly converges to the motor 2 value at the 55th iteration, and the PSO algorithm converges at the 130th iteration. It is also seen that the GA does not converge.



Figure 5. Iteration number versus the fitness value for motor 2.

The slip-torque curves drawn depending on the parameters found by the actual torque values and estimation values are shown in Figures 6 and 7. When examined in terms of the minimum error values, the 4 methods are seen to have caught the actual values with very small differences.

The total error values that occurred in the torque values for motor 1 for each method are shown in Figure 8.



Figure 6. Slip versus torque for motor 1.

Figure 7. Slip versus the torque for motor 2.



Figure 8. Distribution of the total error of the 4 methods for motor 1 (for torque values).

When the total error values given for motor 1 are examined, it is seen that the values obtained by the GA as a result of 31 operations are bigger than the values obtained by the other 3 methods. It is seen that the maximum error value is obtained by the GA at the 30th operation, and the minimum error value is obtained at the 8th operation. It is seen that, after the GA, the biggest error values are obtained by the PSO algorithm. However, the lowest error values are obtained in the parameter estimation done by the DEA and CSS algorithm. In the operations done by the 4 methods, the smallest error value is obtained by the DEA at its 19th operation. However, it is seen that the examined CSS algorithm has values close to those of the DEA, which gives the smallest error values.

The total error values that occurred in the torque values for motor 2 for each method are shown in Figure 9.



Figure 9. Distribution of the total error of the 4 methods for motor 2 (for torque values).

When all of the error values given for motor 2 are examined, it is seen that the values are similar to the distribution of total error obtained for motor 1. While the minimum error value is obtained from the DEA at its 4th operation, the maximum error value is obtained by the GA at its 8th operation. The error value of the CSS algorithm is close to that of the DEA.

The CPU times obtained by the 31 operations of the 4 methods are given in Figures 10 and 11. It is seen that the GA has the longest solution time and the PSO has the shortest solution time. The solution times of the 4 methods are seen to be less than 1 s for both motors.



Figure 10. Distribution of the CPU time of the 4 methods for motor 1.



Figure 11. Distribution of the CPU time of the 4 methods for motor 2.

When Table 4 is examined, it is seen that the maximum total error value is obtained from the GA and the total minimum error value is obtained from the DEA. The CSS algorithm gives the best results after the DEA. When the standard deviation values are examined, the DEA and CSS algorithm have the lowest standard deviation at 31 operations.

Table 4. Comparison of the CSS performance with other the methods for motor 1 (for torque values).

Methods	Maximum error	Average error	Minimum error	Standard deviation
CSS	0.000017208796	0.000005448508	0.00000053554	4.85183e-06
DEA	0.000000193725	0.00000082610	0.00000003131	6.13198e-08
PSO	0.042305520373	0.024503987984	0.003623805767	0.010199809
GA	0.284213252677	0.106073346508	0.019933179330	0.070428281

The equivalent circuit parameters and average percent error values obtained by the DEA and GA in [6] are given comparatively in Table 5, with the values found by the CSS algorithm in this study.

		Reference values [6]			Present study's values		
		DEA		GA		$\mathbf{CSS}$	
Demomster	Actual	Estimation	Error	Estimation	Error	Estimation	Error
Parameters	values	values	(%)	values	(%)	values	(%)
$R_1$	0.087	0.087	0	0.084	3.448	0.082	4.659
$R_2$	0.228	0.238	4.385	0.239	4.824	0.221	2.815
X	0.604	0.631	4.470	0.633	4.801	0.606	0.399
$X_m$	13.08	13.291	1.163	13.304	1.712	13.730	4.973
Average error			2.617		3.696		3.211

Table 5. Comparison of the equivalent circuit parameters (DEA, GA, and CSS).

The error value found by the CSS is seen to converge to the average error value found by the DEA method used in [6]; however, it is seen to converge with a better result than that found by the GA.

When the torque values in Table 6 are considered, the error values found by the CSS are seen to give better results than those found by the DEA and GA.

		Reference values [6]				Present study's values	
		DEA		GA		CSS	
Davamatara	Actual	Estimation	Error	Estimation	Error	Estimation	Error
Parameters	values	values	(%)	values	(%)	values	(%)
$T_{st}$	529.708	531.659	0.368	530.635	0.175	529.708	1.675e-5
$T_{\rm max}$	773.987	776.352	0.305	777.149	0.408	773.986	1.654e-5
$T_n$	234.55	234.863	0.133	235.076	0.224	234.550	8.018e-5
Average error			0.268		0.269		3.782e-5

Table 6. Comparison of the torque values (DEA, GA, and CSS).

### 4. Conclusion

In this study, the CSS algorithm for estimation of the equivalent circuit parameters of an induction motor was applied for the first time in the literature. The obtained results were compared with the DEA, PSO, and GA for 2 different motors. The known equivalent circuit parameters and slip-torque characteristics of wound-rotor motor were obtained from [25] and the required values were taken from these characteristics. For the squirrelcage motor, the equivalent circuit parameters were obtained from [6]. The reason for using the literature data is that the catalog values given by the manufacturer cannot model the motor properly. It is not possible to obtain convergence from the motor catalog values of various manufacturers.

For motor 1, the CSS algorithm and DEA converge faster than the other algorithms. For motor 2, the CSS algorithm catches the optimum point at 55 iterations and the DEA catches the optimum point at 40 iterations. As seen from Figures 6 and 7, the estimated equivalent circuit parameters exactly model the slip-torque characteristics of both motors. From the obtained results, it is observed that if manufacturers give the exact values for motors, the CSS algorithm can estimate the equivalent circuit parameters properly.

This study shows hopeful results that the CSS algorithm can be used to estimate the parameters of other types of electrical machines as well.

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