

## A new algorithm of parameter estimation of a photovoltaic solar panel

Mustapha BELARBI<sup>1,\*</sup>, Amine BOUDGHENE-STAMBOULI<sup>1</sup>,  
El-Habib BELARBI<sup>2</sup>, Kamel HADDOUCHE<sup>3</sup>

<sup>1</sup>Department of Electronics, University of Sciences and Technology of Oran - Mohamed Boudhif, El M'Naouer, Oran, Algeria

<sup>2</sup>Synthesis and Catalysis Laboratory, Ibn Khaldun University, Tiaret, Algeria

<sup>3</sup>Industrial Technologies Laboratory, Ibn Khaldun University, Tiaret, Algeria

Received: 10.08.2013

Accepted/Published Online: 04.11.2013

Final Version: 01.01.2016

**Abstract:** In this paper, we present a new approach for estimating the one-diode model parameters of a photovoltaic solar panel according to the irradiance and temperature. These parameters are given, at a known irradiance and temperature, from the knowledge of three operating points: short circuit, open circuit, and maximum power. In the first step, the adopted approach concerns the resolution of the system of equations constituting the three operating points to write all the model parameters according to series resistance. Secondly, we make an iterative resolution at the optimal operating point by using the Newton–Raphson method to calculate the series resistance value as well as the model parameters. Once the last ones are identified, we consider other equations for taking into account the irradiance and temperature effect. The simulation results show the convergence speed of the model parameters and the possibility of visualizing the electrical behavior of the panel according to the irradiance and temperature. With the identified model, we can develop algorithms of maximum power point tracking and make simulations of PV systems.

**Key words:** Renewable energy, solar, photovoltaic, parameters identification, modeling and simulation, maximum power point tracking

### 1. Introduction

In the recent years, the problem of energy crunch is more and more aggravating. Very much exploitation and research for power energy are carried out around the world. In particular, solar energy attracts much attention. The utilization of photovoltaic (PV) conversion energy is today an emerging technology, characterized by gradually declining costs and increasing acquaintance with the technology.

Solar cells represent the fundamental power conversion unit of a PV system and are usually arranged in a PV array. For this last, the most important information needed from the manufacturer is the module short circuit current, open circuit voltage, and maximum power point current and voltage, all measured at the same irradiance and cell temperature. This information fixes three current-voltage (I-V) points, all of which must lie on the same I-V curve and therefore satisfy the same I-V equations. Both of these equations are implicit and nonlinear and therefore determination of an analytical solution is difficult.

This paper concerns the resolution of the I-V equations for on the one hand identifying the PV panel parameters and, on the other hand, for predicting its behavior under varying conditions such as irradiance and temperature.

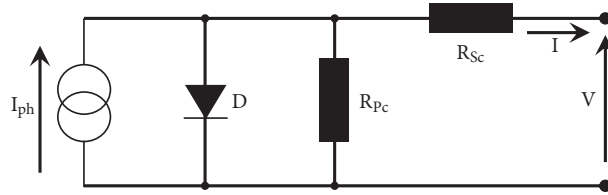
\*Correspondence: [mustapha.belarbi@yahoo.fr](mailto:mustapha.belarbi@yahoo.fr)

## 2. Mathematical model for a photovoltaic cell

For modeling the PV solar panel, one of the two standard models, the one-diode model or the two-diode model, was used to describe the electrical characteristics of the solar cell. Each model establishes relations to evaluate the current and the voltage according to the irradiance and temperature.

The double-exponential model (with two diodes) is derived from the physics of the p-n junction and is generally accepted as reflecting the behavior of such cells, especially those constructed from polycrystalline silicon. It is also suggested that cells constructed from amorphous silicon, usually using thick-film deposition techniques, do not exhibit as sharp a knee in the curve as do the crystalline types, and therefore the one-exponential model (with one diode) provides a better fit to such cells [1,2].

In this work, we consider a prior one-exponential model. The equivalent circuit used is shown in Figure 1.



**Figure 1.** Cell equivalent circuit (one-exponential model).

The relationship between voltage  $V$  [V] and current  $I$  [A] for the one-exponential model is given by the following equation:

$$I = I_{ph} - I_S \left( \exp \left( \frac{q(V + R_{Sc}I)}{\alpha kT} \right) - 1 \right) - \frac{V + R_{Sc}I}{R_{Pc}}, \quad (1)$$

where  $R_{Sc}$  is the series resistance parameter of the cell [ $\Omega$ ],  $R_{Pc}$  is the shunt resistance parameter [ $\Omega$ ],  $\alpha$  is the diode parameter (usually  $\alpha \approx 1.2$ ),  $T$  is the cell temperature [K],  $q$  is the charge of an electron ( $1.6021 \times 10^{-19}$  C),  $k$  is the Boltzmann constant ( $1.3854 \times 10^{-23}$  JK $^{-1}$ ),  $I_{ph}$  is the photocurrent [A], and  $I_S$  is the saturation current [A].

## 3. Irradiance and temperature effects

The I-V characteristic of a solar cell is also influenced by the temperature of the cell. In this work, the cell temperature is calculated by a simplified linear function between the cell temperature and the irradiation  $G$  [Wm $^{-2}$ ]. Eq. (2) below describes the model, where the temperature  $T_a$  determines the crossing point of the function on the vertical axis [3]:

$$T = T_a + 0.03 \cdot G. \quad (2)$$

The photocurrent  $I_{ph}$  is given by:

$$I_{ph} = (C_0 + C_1 \cdot T) \cdot \frac{G}{G^*}, \quad (3)$$

where  $C_0$  is a coefficient that relates the photocurrent to the irradiance [A],  $C_1$  is a coefficient that expresses the relation between the photocurrent and the temperature [AK $^{-1}$ ], and  $G^*$  is the irradiance at the reference conditions [Wm $^{-2}$ ].

The constants  $C_0$  and  $C_1$  are expressed by the following equations:

$$C_0 = \frac{I_{SC1} \cdot T_2 - I_{SC2} \cdot T_1}{T_2 - T_1}, \quad (4)$$

$$C_1 = \frac{I_{SC2} - I_{SC1}}{T_2 - T_1}, \quad (5)$$

where  $I_{SC1}$ ,  $I_{SC2}$  are the short-circuit currents given respectively at the measured temperatures  $T_1$  and  $T_2$ .

The dependence of the saturation current on temperature is given by:

$$I_S = C_3 \cdot T^3 \cdot \exp\left(\frac{-C_2}{T}\right), \quad (6)$$

where the constants  $C_2$  and  $C_3$  are expressed by the following equations:

$$C_2 = \frac{q \cdot E_g}{k}, \quad (7)$$

$$C_3 = \frac{I_{SC1} \cdot \exp\left(\frac{q \cdot E_g}{\alpha k T_1}\right)}{T_1^3 \cdot \left(\exp\left(\frac{q \cdot V_{OC1}}{\alpha k T_1}\right) - 1\right)}, \quad (8)$$

where  $E_g$  is the band gap voltage.

Using Eq. (1), the one-exponential model of the PV array is given as follows:

$$I = I_{ph} - I_S \left( \exp\left(\frac{q(V + R_S I)}{N_C \alpha k T}\right) - 1 \right) - \frac{V + R_S I}{R_P}, \quad (9)$$

where  $R_S$  is the series resistance parameter of the array [ $\Omega$ ],  $R_P$  is the shunt resistance parameter [ $\Omega$ ], and  $N_C$  is the number of cells in series.

The set of model parameters ( $I_{ph}$ ,  $I_S$ ,  $R_S$ , and  $R_P$ ) allows thereafter the layout of the current-voltage curve for different conditions of solar radiation.

The operation point of the PV panel is given by:

$$\begin{cases} V_{panel} = N_S \cdot V \\ I_{Panel} = N_P \cdot I \end{cases}, \quad (10)$$

where  $N_S$  is the number of arrays in series and  $N_P$  is the number of arrays in parallel.

#### 4. Model parameter identification

We remind the reader that the one-exponential model is nonlinear and implicit. Its parameters are given from the knowledge of three operating points: short circuit, open circuit, and maximum power [4–18]. In the first step, the adopted approach concerns the resolution of the system of equations constituting the three operating points to write all the model parameters according to series resistance. Secondly, we make an iterative resolution at the optimal operating point by using the Newton–Raphson method to calculate the series resistance value as well as the model parameters.

Notice that particular attention must be considered for the correct choice of the initial values because inadequate choice of the last ones will have as a consequence the divergence of the algorithm. For the series resistance  $R_S$ , we suppose that initially it is null:

$$R_{S0} = 0. \quad (11)$$

This allows only the launching of the calculation algorithm of the  $I_{ph}$ ,  $I_S$ ,  $R_S$ , and  $R_P$  parameters. If these parameters are known, we can determine from Eq. (9) the current  $I$  of the PV array according to the voltage  $V$ .

Usually, the three operating points given by the manufacturer of the PV array are:

1. Open circuit point:

$$I = 0 \ \& \ V = V_{OC},$$

2. Short-circuit point:

$$I = I_{SC} \ \& \ V = 0,$$

3. Optimal operating point (at maximum power):

$$I = I_{OP} \ \& \ V = V_{OP}.$$

In compact form and after some developments, we can write by taking into account the last three operating points the following system:

$$\begin{bmatrix} I_{ph} \\ I_S \\ R_P^{-1} \end{bmatrix} = [M]^{-1} \cdot \begin{bmatrix} 0 \\ I_{SC} \\ I_{OP} \end{bmatrix}. \quad (12)$$

Matrix  $M$  is related to  $R_S$ ,  $V_T$ ,  $V_{OC}$ ,  $I_{SC}$ ,  $V_{OP}$ , and  $I_{OP}$ , and it is given by:

$$[M] = \begin{bmatrix} 1 & -C & -V_{OC} \\ 1 & -B & -R_S I_{SC} \\ 1 & -A & -V_{OP} - R_S I_{OP} \end{bmatrix}, \quad (13)$$

where  $A$ ,  $B$ , and  $C$  are expressed by the following equations, respectively:

$$A = \exp\left(\frac{q(V_{OP} + R_S I_{OP})}{N_C \alpha k T}\right) - 1, \quad (14)$$

$$B = \exp\left(\frac{q R_S I_{SC}}{N_C \alpha k T}\right) - 1, \quad (15)$$

$$C = \exp\left(\frac{q V_{OC}}{N_C \alpha k T}\right) - 1. \quad (16)$$

Substituting the inverse of the matrix  $M$  into Eq. (12), we can write:

$$\begin{cases} I_{ph} = \frac{V_{OC} I_{SC} A - V_{OC} I_{OP} B - V_{OP} I_{SC} C}{\det_M} \\ I_S = \frac{V_{OC} I_{SC} - V_{OC} I_{OP} - V_{OP} I_{SC}}{\det_M} \\ R_P^{-1} = \frac{I_{SC} A - I_{OP} B - (I_{SC} - I_{OP}) C}{\det_M} \end{cases}, \quad (17)$$

with:

$$\det_M = (V_{OC} - R_S I_{SC})A + (-V_{OC} + V_{OP} + R_S I_{OP})B + (-V_{OP} + R_S(I_{SC} - I_{OP}))C. \quad (18)$$

To calculate the value of  $R_S$ , we must use another equation. The latter is obtained from the derivative of the power. For an optimal operating point, the PV array work at its maximum power and thus the derived power at this point is null. At this point, we can write:

$$\left. \frac{dP}{dV} \right|_{\substack{\text{optimal} \\ \text{operating}}} = 0 \Rightarrow \boxed{\left. \frac{dI}{dV} \right|_{V_{OP}} = -\frac{I_{OP}}{V_{OP}}}. \quad (19)$$

From Eq. (9), the derivative of current can be expressed as below:

$$\frac{dI}{dV} = - \left( R_S + \left( \frac{qI_S}{N_C \alpha k T} \cdot \exp \left( \frac{q(V + R_S I)}{N_C \alpha k T} \right) + \frac{1}{R_P} \right)^{-1} \right)^{-1}. \quad (20)$$

Substituting this equation into Eq. (19), we define the function  $f$  as follows:

$$f = I_{OP} - (V_{OP} - R_S I_{OP}) \cdot \left( \frac{qI_S}{N_C \alpha k T} \cdot \exp \left( \frac{q(V_{OP} + R_S I_{OP})}{N_C \alpha k T} \right) + \frac{1}{R_P} \right) = 0. \quad (21)$$

As  $I_S$  and  $R_P$  are related to  $R_S$ , the function  $f$  is also related to it. The Newton–Raphson method is used for solving the equation  $f(R_S) = 0$ . Note that the method is commonly used because of its simplicity and great speed.

The derivative of the function  $f$  is given by the following equation:

$$\begin{aligned} \frac{df}{dR_S} = & -\frac{(V_M - R_S I_M)}{det_M} \frac{qI_M I_{SC}}{N_C \alpha k T} (A - B) + \frac{1}{R_P} \left( I_M + \frac{(V_M - R_S I_M)}{det_M} \frac{d det_M}{d R_S} \right) \\ & + \frac{qI_S}{N_C \alpha k T} \exp \left( \frac{q(V_M + R_S I_M)}{N_C \alpha k T} \right) \cdot \left( I_M \left( 1 - \frac{q(V_M - R_S I_M)}{N_C \alpha k T} \right) + \frac{V_M - R_S I_M}{det_M} \cdot \frac{d det_M}{d R_S} \right), \end{aligned} \quad (22)$$

where  $det_M$  is the determinant of the matrix  $M$ ; its derivative is given by:

$$\begin{aligned} \frac{d det_M}{d R_S} = & \left( \frac{q(V_{OC} - R_S I_{SC}) I_M}{N_C \alpha k T} - I_{SC} \right) A + \left( \frac{q(-V_{OC} + V_M + R_S I_M) I_{SC}}{N_C \alpha k T} + I_M \right) B \\ & + (I_{SC} - I_M) C + \frac{q(V_M I_{SC} - V_{OC} (I_{SC} - I_M))}{N_C \alpha k T}. \end{aligned} \quad (23)$$

The developed algorithm can be summarized as in the scheme of Figure 2.

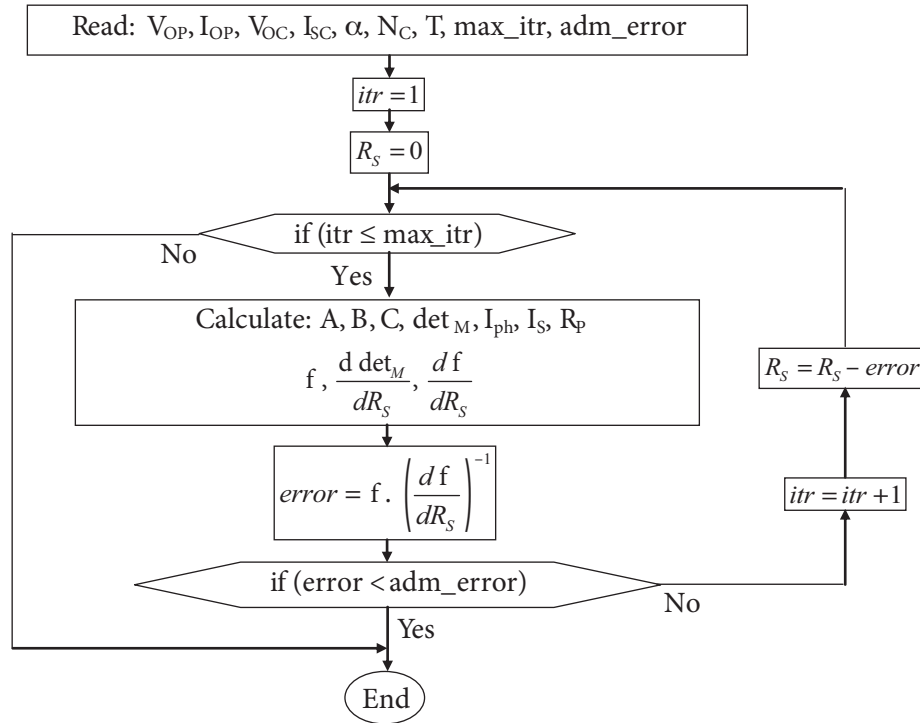


Figure 2. Design of the developed algorithm.

### 5. Simulation results

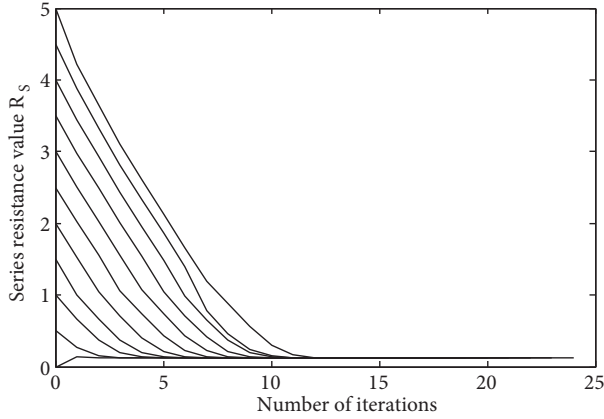
The electrical specifications of the chosen PV array are:

- Module Kyocera: Model KC 50
- Maximum power: 50 W
- Maximum power voltage: 16.7 V
- Maximum power current: 3 A
- Open circuit voltage: 21.5 V
- Short circuit current: 3.1 A
- Number of cells: 36

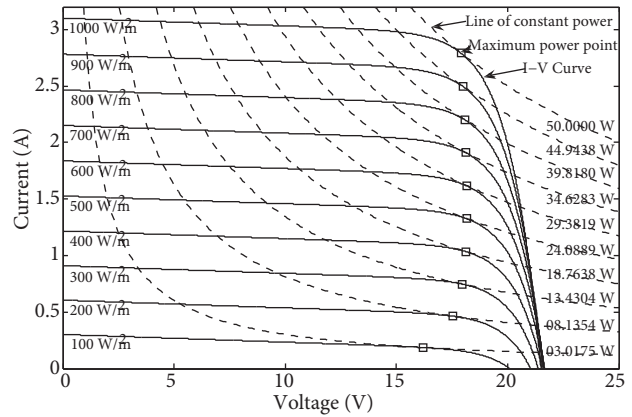
These electrical specifications are obtained under test conditions of irradiance of 1 kW/m<sup>2</sup> and cell temperature of 25 °C. Note that  $E_g$  is equal to 1.12 V.

After several tests of simulation, the computation solution of the series resistance converges after a number of iterations according to the admissible error and the initial value of  $R_S$ . For example, the solution converges after three iterations for an admissible error that is equal to  $10^{-3}$ , and after 14 iterations for an admissible error equal to  $10^{-15}$ . Figure 3 shows the speed convergence for various initial values of the series resistance  $R_S$ .

The calculated current-voltage characteristics for the PV array utilizing the developed algorithm are presented in Figure 4 for different conditions of solar radiation. In the plot the points of maximum power for each irradiance and the lines of constant power are also indicated.



**Figure 3.** Speed convergence of the series resistance.



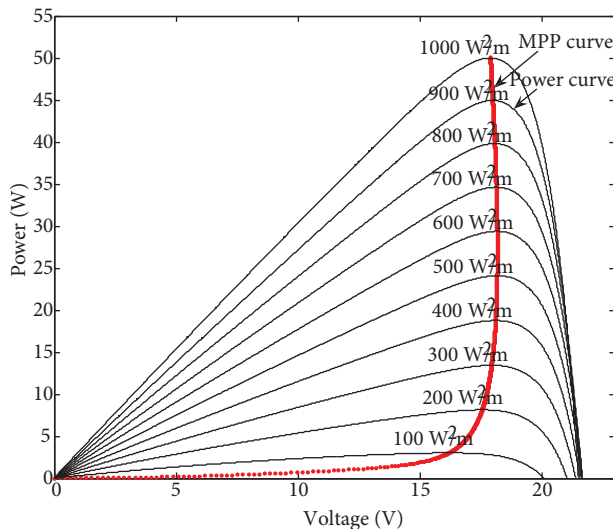
**Figure 4.** The simulated I-V curves for different irradiation conditions.

From Figure 4, we see that the I-V characteristic of the PV array is not stable, and thus it is strongly related to the irradiance.

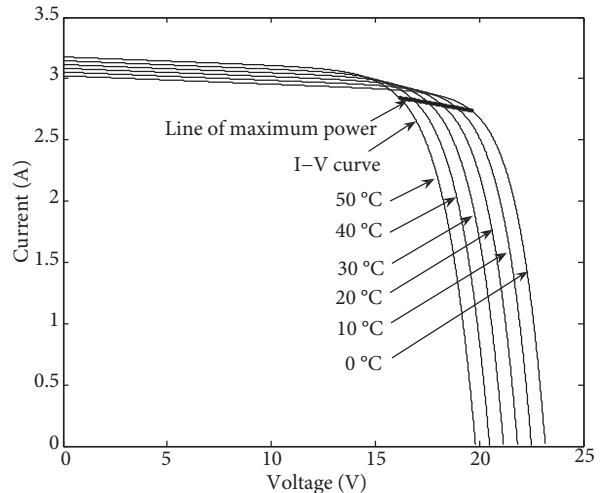
The simulated output power curves of the PV array are given in Figure 5.

For the output power, we note that from certain irradiance the value of the optimal voltage is practically constant.

The effect of the temperature on the electrical behavior of the PV array is given in Figures 6 and 7.



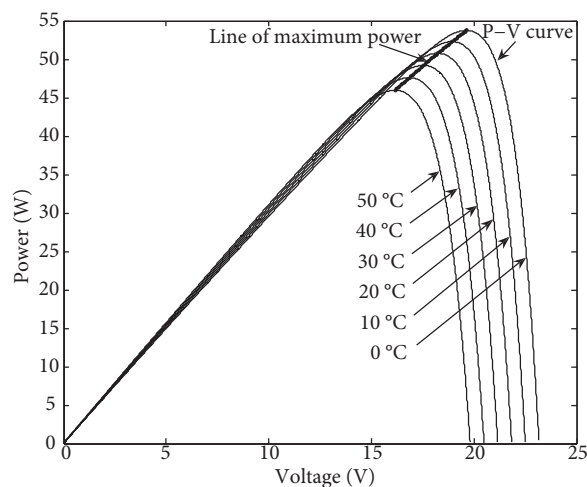
**Figure 5.** Output power of the PV array for different irradiances.



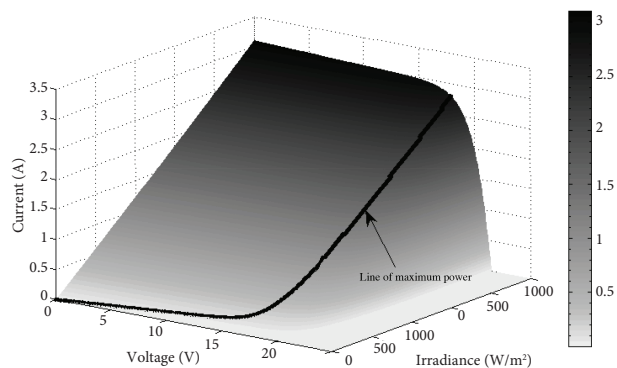
**Figure 6.** The simulated I-V curves for different temperatures.

We note that the increase in temperature leads to a small increase in current but an important fall of the voltage, and thus a fall of the produced power.

In Figure 8, we show the effect of the irradiance on I-V characteristics in 3D representation as well as the line of optimal operating.



**Figure 7.** Output power of the PV array for different temperatures.



**Figure 8.** Current-voltage characteristics in 3D representation.

It should be noted that for these simulations, we consider that the panel contains one module (i.e.  $N_S = N_P = 1$ ).

## 6. Conclusion

In this paper, we presented the modeling and the simulation of the electrical behavior of a PV panel according to the irradiance and temperature.

We developed an algorithm for estimating the one-exponential model parameters of the PV array. These parameters were identified from the knowledge of three operating points given by the manufacturer. The speed convergence of the solution provided by the developed algorithm depends on the choice of the initial value of  $R_S$  and the admissible error. Let us note that the sensitivity of the algorithm for the optimal operating point was noted owing to the fact that a small variation of the value of the optimal voltage leads to a very great variation of the values of the identified parameters.

The simulation results showed the effectiveness of the developed algorithm for calculating the model parameters and the possibility of visualizing the electrical behavior of the PV panel according to the irradiance and the temperature.

## References

- [1] Gow JA, Manning CD. Development of a photovoltaic array model for use in power-electronics simulation studies. IEE P-Elect Pow Appl 1999; 146: 193–200.
- [2] Townsend TU. A method for estimating the long-term performance of direct-coupled photovoltaic systems. MSc, University of Wisconsin, Madison, WI, USA, 1989.
- [3] Moraes-Duzat R. Analytical and experimental investigation of photovoltaic pumping systems. DSc, University of Oldenburg, Oldenburg, Germany, 2000.



- [4] Attivissimo F, Adamo F, Carullo A, Lanzolla AML, Spertino F, Vallan A. On the performance of the double-diode model in estimating the maximum power point for different photovoltaic technologies. *Measurement* 2013; 46: 3549–3559.
- [5] Sissoko G, Mbodji S. A method to determine the solar cell resistances from single I-V characteristic curve considering the junction recombination velocity. *Int J Pure Appl Sci Technol* 2011; 6: 103–114.
- [6] Can H. Model of a photovoltaic panel emulator in MATLAB-Simulink. *Turk J Electr Eng Co* 2013; 21: 301–308.
- [7] El-Tayyan A. A simple method to extract the parameters of the single-diode model of a PV system. *Turk J Phys* 2013; 37: 121–131.
- [8] Bastidas JD, Franco E, Petrone G, Ramos-Paja CA, Spagnuolo G. A model of photovoltaic fields in mismatching conditions featuring an improved calculation speed. *Electr Pow Syst Res* 2013; 96: 81–90.
- [9] El-Naggar KM, AlRashidi MR, AlHajri MF, Al-Othman AK. Simulated annealing algorithm for photovoltaic parameters identification. *Sol Energy* 2012; 86: 266–274.
- [10] Zhu XG, Fu ZH, Long XM, Li X. Sensitivity analysis and more accurate solution of photovoltaic solar cell parameters. *Sol Energy* 2011; 85: 393–403.
- [11] Kashif I, Zainal S, Hamed T, Amir S. A critical evaluation of EA computational methods for photovoltaic cell parameter extraction based on two diode model. *Sol Energy* 2011; 85: 1768–1779.
- [12] Kashif I, Zainal S, Syafaruddin. A comprehensive MATLAB Simulink PV system simulator with partial shading capability based on two-diode model. *Sol Energy* 2011; 85: 2217–2227.
- [13] ] Kashif I, Zainal S. An improved modeling method to determine the model parameters of photovoltaic modules using differential evolution. *Sol Energy* 2011; 85: 2349–2359.
- [14] Kashif I, Zainal S, Hamed T, Amir S. Simple, fast and accurate two-diode model for photovoltaic modules. *Sol Eng Mat Sol C* 2011; 95: 586–594.
- [15] Rodrigues EMG, Melicio R, Mendes VMF, Catalão JPS. Simulation of a solar cell considering single-diode equivalent circuit model. In: *ICREPQ'11 International Conference on Renewable Energies and Power Quality*; 13–15 April 2011; Las Palmas de Gran Canaria, Spain. pp. 1–5.
- [16] Zainal S, Kashif I, Hamed T. An improved two-diode photovoltaic model for PV system. In: *PEDES'10 International Conference on Power Electronics Drives and Energy Systems*; 20–23 December 2010; New Delhi, India. pp. 1–5.
- [17] Chang CH, Zhu JJ, Tsai HF. Model-based performance diagnosis for PV systems. In: *SICE'10 Annual Conference*; 18–21 August 2010; Taipei, Taiwan. pp. 2139–2145.
- [18] Adamo F, Attivissimo F, Di Nisio A, Lanzolla AML, Spadavecchia M. Parameters estimation for a model of photovoltaic panels. In: *XIX IMEKO World Congress Fundamental and Applied Metrology*; 6–11 September 2009; Lisbon, Portugal. pp. 964–967.