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# A new electronically tunable first-order all-pass filter using only three NMOS transistors and a capacitor 

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#### Abstract

In this paper, a new first-order voltage-mode (VM) all-pass filter that consists of only three NMOS transistors and a capacitor is proposed. The resonance frequency of the proposed circuit can be tuned electronically by a control current. It has high input impedance; thus, it can be easily cascaded with other VM circuits. Furthermore, it does not require any critical passive component matching conditions. Nevertheless, it does not have low output impedance. Although a floating capacitor is used in the proposed circuit, it can be easily realized with today's technologies. Ideal and nonideality analyses are performed for the proposed circuit. The behavior of the filter is verified by a number of SPICE simulations and an experimental test. The total harmonic distortion variations of the proposed circuit are found low enough.


Key words: All-pass filter, voltage-mode, NMOS

## 1. Introduction

All-pass filters (APFs) are widely used in a number of analog signal processing applications to provide phase linearity, phase shifting, signal delay processes, etc. APFs can be classified according to their operating mode such as voltage mode (VM) and current mode (CM). Some VM APFs are composed of MOS transistors [1-8]. A CM APF employs a number of MOS transistors [9]. On the other hand, the VM APFs in [10-15] contain active building blocks using tens of MOS transistors. The circuits implemented by a reduced number of transistors are given in $[5,6]$, but they include several passive elements. The main property of VM filters is their cascadability, and thus they should have the property of high input impedance [3,7,10-14]. APFs can be tuned electronically as given in $[2-4,7,8]$. However, some APFs require bias voltage(s) [1,2,5,9]. The APF in [7] has high input impedance and it uses five NMOS transistors. The APF circuits in [8,9] consist of only one passive element, but they respectively contain six and seven MOS transistors. The circuit in [8] does not have high input impedance. The gains of the APFs in $[2,6]$ are less than unity.

In the present work, a novel VM first-order APF employing only three NMOS transistors and a capacitor is proposed. The pole frequency of the proposed APF can be adjusted by changing the value of the control current. One of the main properties of the proposed APF is its high input impedances; thus, it can be easily cascaded with other VM circuits. Moreover, it does not need any critical passive element matching constraints. However, it does not have low output impedance. It consists of a floating capacitor, which can be easily realized

[^0]with today's IC technologies [16]. A number of time domain and frequency domain simulations and experimental test results are included to verify the claimed theory.

The paper is organized as follows: after the introduction in Section 1, the proposed APF structure is treated in Section 2; simulation results for the proposed APF circuit are given in Section 3; in Section 4 experimental test results are provided; and some conclusive remarks are drawn in Section 5.

## 2. The proposed NMOS-based APF

The proposed first-order VM APF circuit is shown in Figure 1. It consists of only three NMOS transistors, $M_{1}-M_{3}$, one capacitor, and a control current, $I_{o}$. the $M_{1}$ and $M_{3}$ transistors behave like a unity gain inverting amplifier [7]. Thus, the drain voltage of $M_{3}$ transistor $V_{D 3}=-V_{i n}$. For the circuit in Figure 1, the equation can be ideally written as:


Figure 1. Proposed APF circuit.

$$
\begin{equation*}
\left(V_{i n}-V_{a p}\right) g_{M_{2}}=\left(V_{a p}-\left(-V_{i n}\right)\right) s C \tag{1}
\end{equation*}
$$

where $g_{M 2}$ is the conductance of $M_{2}$ and is defined as:

$$
\begin{equation*}
g_{M_{2}}=\sqrt{2 k_{n_{2}} I_{o}} \tag{2}
\end{equation*}
$$

Here, $k_{n}=\mu_{n} C_{o x}(W / L)_{2}$ is the transconductance parameter of the NMOS transistor, $\mu_{n}$ is the mobility of the NMOS transistor, $C_{o x}$ is the gate oxide capacitance per unit area, $W$ is the channel width, and $L$ is the channel length.

From Eq. (1), the transfer function (TF) of the proposed APF is found as:

$$
\begin{equation*}
\frac{V_{a p}}{V_{i n}}=\frac{1-\frac{s C}{g_{M_{2}}}}{1+\frac{s C}{g_{M_{2}}}} \tag{3}
\end{equation*}
$$

which provides noninverting first-order all-pass responses with $\omega_{o}=g_{M 2} / C$. The phase response is evaluated as follows:

$$
\begin{equation*}
\phi(\omega)=-2 \tan ^{-1}\left(\frac{\omega C}{g_{M_{2}}}\right) \tag{4}
\end{equation*}
$$

where the phase changes from $0^{\text {circ }}$ to $-180^{\text {circ }}$ as the frequency varies from zero to infinity. Parasitic impedance $Z_{x}$ can be defined as:

$$
\begin{equation*}
Z_{x}=R_{x} \| \frac{1}{s C_{x}} \tag{5}
\end{equation*}
$$

Here, $R_{x}$ and $C_{x}$ are respectively parasitic resistor and capacitor, which are computed as follows:

$$
\begin{gather*}
R_{x}=\frac{1}{g_{M_{1}}}\left\|r_{o 1}\right\| r_{o 3}  \tag{6}\\
C_{x} \cong C_{g s 1}+C_{d s 1}+C_{g d 3}+C_{d s 3} \tag{7}
\end{gather*}
$$

TF of the proposed APF with parasitic impedances is obtained as:

$$
\begin{equation*}
\frac{V_{a p}}{V_{i n}}=\frac{g_{M_{2}}-\frac{s C\left(1+s C_{x} R_{x}\right)}{1+s\left(C+C_{x}\right) R_{x}}}{g_{M_{2}}+\frac{s C\left(1+s C_{x} R_{x}\right)}{1+s\left(C+C_{x}\right) R_{x}}} \tag{8}
\end{equation*}
$$

From Eq. (8), for proper operation of the first proposed APF, the following constrains should be satisfied:

$$
\begin{gather*}
\omega C_{x} R_{x} \ll 1  \tag{9}\\
\omega\left(C+C_{x}\right) R_{x} \ll 1 \tag{10}
\end{gather*}
$$

From Eq. (8), the following useful operating frequency range is obtained:

$$
\begin{equation*}
f \leq \frac{0.1}{2 \pi} \frac{1}{\left(C+C_{x}\right) R_{x}} \tag{11}
\end{equation*}
$$

It is important to note that $1 / g_{M 2} \ll r_{o 2}$ should be chosen for proper operation of the proposed APF, which can be achieved by choosing a larger length of the $M_{2}$ transistor [17].

## 3. Simulation results

The proposed APF is simulated by using 0.13 mu m IBM CMOS technology parameters in SPICE program. DC symmetrical power supply voltages are chosen as $V_{D D}=-V_{S S}=0.75 \mathrm{~V}$. All the bulks of the NMOS transistors are connected to relevant sources. Dimensions of the NMOS transistors are given in Table 1. We prefer 0.13 mu m deep submicron technology because of its low power dissipation and DC symmetrical power supply voltages.

Table 1. Dimensions of the NMOS transistors.

| Transistor name | Aspect ratio $(W / L)$ |
| :--- | :--- |
| $M_{1}$ and $M_{3}$ | $130 / 0.52 m u \mathrm{~m}$ |
| $M_{2}$ | $1.3 / 0.52 \mathrm{mu} \mathrm{m}$ |

In simulations, $R_{x}$ in Figure 1 is calculated as $25.54 \Omega$ and $C_{x}$ is found as 416 fF . The gain and phase responses of the proposed APF with $I_{o}$ variations are depicted in Figure 2, where $C=10 \mathrm{pF}$ is selected. The gain response of the proposed APF is approximately equal to -1 dB , which is acceptable.


Figure 2. The gain and phase response of the proposed APF circuit.
The control current $I_{o}$ is selected as 100 mu A for all simulations below and $C=10 \mathrm{pF}$ is selected, which yields a pole frequency of 5.52 MHz . A sinusoidal input signal with a peak value of 10 mV at a frequency of 5.52 MHz is applied to show the time domain performance of the proposed APF. The input and corresponding output are given in Figure 3, where a phase difference of about $90^{\text {circ }}$ between the input and output signals at pole frequency is seen.

The gain and phase responses of the proposed APF circuit are given in Figure 4, where only the width of the $M_{2}$ transistor in Figure 1 is varied between 1.04 mu m and 1.56 mu m by a step size of 0.13 mu m . Additionally, a sinusoidal input signal with a peak value of 10 mV at 5.52 MHz is applied. The input and corresponding output voltages of the proposed APF circuit are drawn in Figure 5, in which only the width of the $M_{2}$ transistor in Figure 1 is varied between $1.04 m u \mathrm{~m}$ and 1.56 mu m by a step size of 0.13 mu m . By varying the $M_{2}$ transistor width, the change in gain is slight and offset voltages occur.


Figure 3. Input and corresponding output of the proposed APF at a frequency of 5.52 MHz .

A Monte Carlo analysis with twenty runs with $5 \%$ variations of the $V_{T H 0}$ is performed by applying a sinusoidal input signal with a peak value of 10 mV at 5.52 MHz . The result is shown in Figure 6. In this analysis, it is seen that offset voltages occur when the $V_{T H 0}$ value is changed.

To show the frequency domain and time domain responses of the proposed APF, Monte Carlo analyses with twenty runs for $20 \%$ variations of the capacitor $C$ are given in Figures 7 and 8, respectively. The input and output noises of the proposed APF circuit are shown in Figure 9, which are adequately low values. The
total harmonic distortion (THD) variations with respect to the peak value of the applied sinusoidal signal at a frequency of 5.52 MHz are depicted in Figure 10, where it can be seen that THD variations are smaller than $1 \%$.


Figure 5. Input and corresponding output of the proposed APF by changing $W$ of transistor $M_{2}$.


Figure 7. Monte Carlo analysis of the proposed APF circuit in the frequency domain by changing the $C$ value.


Figure 9. The input and output noises of the proposed APF.


Figure 6. Monte Carlo analysis of the proposed APF circuit by changing the $V_{T H 0}$ value.


Figure 8. Monte Carlo analysis of the proposed APF circuit in the time domain by changing the $C$ value.


Figure 10. THD against the peak value of the applied sinusoidal signal for the proposed APF.

The total power dissipation of the proposed circuit is approximately 20.6 mW in SPICE simulations. Moreover, the CMOS-based first-order APF circuits in the literature and the proposed one are compared in Table 2: the proposed APF has high input impedance and tunability, and a low number of active and passive
elements. As an example, when compared with the filter configuration in [7] employing five NMOS transistors, the circuit of the present work consists of only three NMOS transistors. Nonetheless, the circuit of the present work has a floating capacitor and does not have low output impedance.

Table 2. A comparison table of MOS transistor-based APF circuits.

| References | \# of <br> transistors | \# of passive <br> passive elements | High Input <br> Impedance | Tunability | Bias <br> requirement(s) | Technology | Power <br> supplies |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $[\mathbf{1}]$ | 6 | 2 | No | No | Yes | $0.35 \mu \mathrm{~m}$ | 3.3 V |
| $[\mathbf{2}]$ | 9 | 3 | No | Yes | Yes | $0.35 \mu \mathrm{~m}$ | $\pm 1.5 \mathrm{~V}$ |
| $[\mathbf{3}]$ | tens | 1 | Yes | Yes | No | $0.25 \mu \mathrm{~m}$ | 2.5 V |
| $[\mathbf{4}]$ | 5 | 1 | No | Yes | No | $0.35 \mu \mathrm{~m}$ | $\pm 1.5 \mathrm{~V}$ |
| $[\mathbf{5}]$ | 3 | 3 | No | No | Yes | $0.35 \mu \mathrm{~m}$ | $\pm 1.5 \mathrm{~V}$ |
| $[\mathbf{6}]$ | 2 | 4 | No | No | No | $0.18 \mu \mathrm{~m}$ | $\pm 0.9 \mathrm{~V}$ |
| $[\mathbf{7}]$ | 5 | 1 | Yes | Yes | No | $0.18 \mu \mathrm{~m}$ | $\pm 0.9 \mathrm{~V}$ |
| $[\mathbf{8}]$ | 6 | 1 | No | Yes | No | $0.18 \mu \mathrm{~m}$ | $\pm 0.9 \mathrm{~V}$ |
| This work | 3 | 1 | Yes | Yes | No | 0.13 mu m | $\pm 0.75 \mathrm{~V}$ |

## 4. Experimental results

The proposed APF in Figure 1 can be realized by three commercially available discreet NMOS transistors such as 2 N 7000 for an experimental test. Additionally, to generate control current $I_{o}$, a voltage to current converter circuit in Figure 11 employing only one AD 844 device, and a resistor, $R=10 \mathrm{k} \Omega$, is used. The input voltage of the circuit in Figure 11 is chosen as -1 V . Thus, $I_{o}$ is obtained as 100 mu A. The passive component $C$ of the experiment test circuit is selected as 1 nF . Furthermore, the DC symmetrical power supply voltages are chosen as $\pm 2.5 \mathrm{~V}$. An experimental test is achieved applying a sinusoidal input voltage with a peak to peak amplitude of 200 mV at different frequency values. The gain and phase responses of the experimental test circuit are given in Figure 12. The pole frequency $f_{o}$ is approximately 86 kHz .


Figure 11. Control current generating circuit.


Figure 12. Frequency response of the experimental test circuit.

The simulation and experimental test results confirm the claimed theory well. The difference among ideal, simulation, and experimental results can be attributed to the nonidealities of the NMOS transistors. Moreover, the parasitics of the board affect the performance of the circuit in experimental testing.

## 5. Conclusion

This paper presents a novel first-order APF employing only three NMOS transistors and a capacitor. The main advantage of the proposed APF is its high input impedance, and thus it can be cascaded with other VM

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circuits easily. Its pole frequency can be tuned electronically by a control current. Moreover, it does not require any critical passive component matching conditions and cancellation constraints. It does not have low output impedance and has a floating capacitor. Simulation and experimental test results confirm the theory well, as expected.

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