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# PENDANT <sup>13</sup>C NMR Spectroscopy Applied to $CH_n$ Groups

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#### Abstract

Polarization enhancement nurtured during attached nucleus testing (PENDANT) NMR spectroscopy gives signals of quaternary carbon atoms in addition to signals indicative of CH, CH<sub>2</sub> and CH<sub>3</sub> groups. In this study, using product operator theory, analytical description of PENDANT NMR spectroscopy for CH<sub>n</sub> ( $IS_n$ ,  $I = \frac{1}{2}$ ,  $S = \frac{1}{2}$ , n = 0, 1, 2, 3) spin systems are presented. Simulation and experimental results of PENDANT NMR spectroscopy are also presented. Theoretical results are found to be in exact agreement with the simulation results and in good agreement with the experimental ones.

Key Words: PENDANT, <sup>13</sup>C NMR, Product Operator Theory.

# 1. Introduction

There exists a large number of one and two-dimensional NMR techniques for  ${}^{13}$ C spectral editing such as attached proton test (APT), sub spectral editing with a multiple quantum trap (SEMUT), distortionless enhancement by polarization transfer (DEPT), polarization enhancement nurtured during attached nucleus testing (PENDANT). PENDANT NMR spectroscopy has to its advantage that it is also capable of detecting quaternary carbon atoms in addition to the signals of CH, CH<sub>2</sub> and CH<sub>3</sub> groups [1, 2].

The product operator formalism, as a simple quantum mechanical method, is widely used for the analytical description of multiple pulse NMR experiments on weakly coupled spin systems in liquids [see e.g., 3-8]. PENDANT NMR spectroscopy of CH<sub>n</sub> groups have been observed for  $d_3 = \frac{5}{8}J$  [1, 9]. In this study, by using product operator theory, an analytical description of PENDANT NMR spectroscopy for CH<sub>n</sub> ( $IS_n$ ,  $I = \frac{1}{2}$ ,  $S = \frac{1}{2}$ , n = 0, 1, 2, 3) spin systems are presented. Simulation and experimental results of PENDANT NMR spectroscopy are also presented for these spin systems. Theoretical results were found to be in exact agreement with the simulation results and in good agreement with the experimental results.

# 2. Theory

Time dependency of the density matrix is given by [6, 7]

$$\sigma(t) = \exp(-iHt)\sigma(0)\exp(iHt),\tag{1}$$

where H is the total Hamiltonian which consists of radio frequency (RF) pulse, chemical shift and spin-spin coupling Hamiltonians and  $\sigma(0)$  is the density matrix at t = 0. After employing the Hausdorff formula [6, 7], we get

$$\exp\left(-iHt\right)A\exp\left(iHt\right) = A - (it)[H, A] + \frac{(it)^{2}}{2!}[H, [H, A]] - \frac{(it)^{3}}{2!}[H, [H, A]] + \dots,$$
(2)

From which the RF pulse, chemical shift and spin-spin coupling evolution of product operators can easily be obtained. Details on the evolution of product operators under these Hamiltonians can be found elsewhere [3, 5–8]. At any time during the experiment, the ensemble averaged expectation value of the spin angular momentum, e.g. for  $I_y$ , is

$$\langle I_y \rangle = Tr \left( I_y \sigma \left( t \right) \right),\tag{3}$$

where  $\sigma(t)$  is the density matrix operator calculated from equation (1) at time t. As  $\langle I_y \rangle$  is proportional to the magnitude of the y-axis magnetization, it represents the signal detected on y-axis. So, in order to estimate the free induction decay (FID) signal of a multiple-pulse NMR experiment, one should obtain density matrix operator at the end of the experiment.

## 3. Results and Discussion

#### **3.1.** Product operator theory

In this section, we present an analytical description of PENDANT NMR spectroscopy for  $IS_n$  spin systems (CH<sub>n</sub> groups) using product operator theory. The pulse sequence employed for PENDANT is illustrated in Figure 1. Optimum value of  $d_2$  is  $(\frac{1}{4}J)$  [9]. Density matrix operator at each stage of the experiment is numerically labeled. We treat <sup>13</sup>C as spin I and <sup>1</sup>H as spin S. So CH<sub>n</sub> groups can be represented as  $IS_n$  ( $I = \frac{1}{2}$ ,  $S = \frac{1}{2}$ ) spin systems.



Figure 1. The pulse sequence for <sup>13</sup>C PENDANT NMR spectroscopy [1,9]. BB: Broad band.

For an IS spin system,  $\sigma_o$  is the density matrix operator at thermal equilibrium and  $\sigma_o = S_z$ . The pulse sequence in Figure 1 (where  $d_2 = \frac{1}{4}J$ ) obviously leads to the following density matrices for each labeled point:

$$\sigma_1 = -S_y,\tag{4}$$

$$\sigma_2 = -S_y \cos\left(\pi J d_2\right) + 2I_z S_x \sin\left(\pi J d_2\right) \tag{5}$$

$$\sigma_3 = S_y \cos\left(\pi J d_2\right) - 2I_z S_x \sin\left(\pi J d_2\right) \tag{6}$$

$$\sigma_4 = -2I_z S_x \tag{7}$$

$$\sigma_5 = 2I_x S_z \tag{8}$$

$$\sigma_6 = 2I_x S_z C_J + I_y S_J. \tag{9}$$

Here and in the following equations  $C_{nJ} = \cos(n\pi J d_3)$ ,  $S_{nJ} = \sin(n\pi J d_3)$  and  $C_I = \cos(\Omega_I t)$ . So we obtain

$$\sigma_8 = -2I_x S_z C_{2J} - I_y S_{2J}.$$
 (10)

Under the chemical shift evolution during time t, the density matrix becomes

$$\sigma_9 = -I_y S_{2J} C_I. \tag{11}$$

For an IS spin system, only the observable  $I_y$  terms are kept in  $\sigma_9$ . For detection along the y-axis, magnetization along the y-axis is proportional to  $\langle I_y \rangle$  and we have

$$M_y(t)\alpha\langle I_y\rangle = Tr\left(I_y\sigma_9\right)$$
  
=  $-S_{2J}C_ITr(I_yI_y).$  (12)

For an IS ( $I=1\!\!/_2$  ,  $S=1\!\!/_2)$  spin system, since  $Tr(I_yI_y)=1,$  we obtain

$$\langle I_{y} \rangle (IS) = -\sin\left(\pi J d_{3}\right) \cos\left(\Omega_{I} t\right).$$
<sup>(13)</sup>

By using the same pulse sequence for the  $I\!S_2$  spin system, we obtain

$$\sigma_o = S_{1z} + S_{2z} \tag{14}$$

$$\sigma_5 = 2I_x S_{1z} + 2I_x S_{2z} \tag{15}$$

and

$$\sigma_9 = -I_y \sin\left(4\pi J d_3\right) \cos\Omega_I t. \tag{16}$$

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Since  $Tr(I_y I_y) = 2$ , we have

$$\langle I_{y} \rangle \left( IS_{2} \right) = -2\sin\left(4\pi Jd_{3}\right)\cos\left(\Omega_{I}t\right).$$

$$\tag{17}$$

Applying the same procedure for  $IS_3$  spin system we obtained

$$\sigma_o = S_{1z} + S_{2z} + S_{3z},\tag{18}$$

$$\sigma_5 = 2I_x S_{1z} + 2I_x S_{2z} + 2I_x S_{3z} \tag{19}$$

and

$$\langle I_y \rangle (IS_3) = -\{3\sin(6\pi J d_3) + 3\sin(2\pi J d_3)\}\cos(\Omega_I t),$$
(20)

where  $Tr(I_y I_y) = 4$  is used.

For IS<sub>n</sub> spin systems values of  $\langle I_y \rangle = Tr(I_y \sigma_9)$  and their normalized forms by multiplication with 4/Tr(E) are given in Table 1, apart from  $\cos(\Omega_I t)$ . Here E is the unity product operator for corresponding spin system. Values of  $\langle I_y \rangle = Tr(I_y \sigma_9)$  represent the FID signals of PENDANT NMR spectroscopy for IS<sub>n</sub> spin system.

**Table 1.**  $\langle I_y \rangle = Tr(I_y \sigma_9)$  values and their normalized forms for IS<sub>n</sub> spin systems apart from  $\cos(\Omega_I t)$  product.

Spin System	$\left\langle I_{y}\right\rangle =Tr\left(I_{y}\sigma_{8}\right)$	$\frac{4}{Tr(E)}$	$\frac{4}{Tr(E)}Tr\left(I_y\sigma_8\right)$
CH(IS)	$-\sin\left(2\pi Jd_3\right)$	1	$-\sin\left(2\pi Jd_3\right)$
$\operatorname{CH}_2(\operatorname{IS}_2)$	$-2\sin\left(4\pi Jd_3\right)$	1/2	$-\sin\left(4\pi Jd_3\right)$
$\mathrm{CH}_3(\mathrm{IS}_3)$	$-3[\sin{(6\pi Jd_3)} + \sin{(2\pi Jd_3)}]$	1/4	$-\frac{3}{4}[\sin{(6\pi Jd_3)} + \sin{(2\pi Jd_3)}]$

The relative signal intensity plots of <sup>13</sup>C PENDANT NMR spectroscopy for CH, CH<sub>2</sub> and CH<sub>3</sub> groups are given in Figure 2 as a function of time,  $d_3$ . As one can see, PENDANT experiment for CH<sub>n</sub> groups can be performed for different  $d_3$  values and the signals of C, CH, CH<sub>2</sub> and CH<sub>3</sub> groups can be identified. Quaternary carbons will always give a negative signal, as they do not depend on the time,  $d_3$ . The expected signs of PENDANT NMR signals of CH<sub>n</sub> groups for different  $d_3$  values obtained from Figure 2 are given in Table 2.



Figure 2. The relative signal intensity plots for <sup>13</sup>C PENDANT NMR spectroscopy for CH, CH<sub>2</sub> and CH<sub>3</sub> groups.

Group	$d_3 = 3/(8J)$	$d_3 = 5/(8J)$	$d_3 = 6/(8J)$	$d_3 = 4/(8J)$
С	—	—	—	_
CH	—	+	+	No signal
$\mathrm{CH}_2$	+	—	No signal	No signal
$CH_3$	_	+	No signal	No signal

Table 2. The expected signs of PENDANT NMR signals of  $CH_n$  groups at different  $d_3$  values.

## 3.2. Simulation

Simulations of PENDANT NMR spectroscopy were performed using the NMR-Sim program. In simulation, an artificial spin system was established with the following chemical shift values: C (60 ppm), CH (50 ppm), CH<sub>2</sub>(40 ppm) and CH<sub>3</sub> (30ppm). The simulated PENDANT spectra are shown in Figure 3 for different values of  $d_3$ . They are in exact agreement with theoretical results presented in Figure 2 and Table 2.



Figure 3. Simulated PENDANT <sup>13</sup>C NMR spectra for different  $d_3$  values: (a) 3/(8J), (b) 5/(8J), (c) 6/(8J) and (d) 4/(8J).

#### **3.3.** Experimental results

Experimental measurements are performed using a Bruker DRX-400 NMR Spectrometer using 50% Crotonic acid ethyl ester (I). The <sup>1</sup>H broad band decoupled <sup>13</sup>C NMR spectrum of this sample is shown in Figure 4(a). <sup>13</sup>C PENDANT NMR spectra obtained for  $d_3 = 3/(8J)$  and 5/(8J) are shown in Figures 4(b) and 4(c). Experimental spectra obtained for  $d_3 = 6/(8J)$  and 4/(8J) values are not in agreement with theory and simulation. So they are not presented here. This is because spin–spin coupling constants are different for CH, CH<sub>2</sub> and CH<sub>3</sub> groups. The experimental results obtained for  $d_3 = 3/(8J)$  and 5/(8J) are shown in 5/(8J) are in agreement with theory (Figure 2 and Table 2) and simulation (Figure 3). These values can be called

optimum values for this experiment as all groups give signals of maximum intensity. For these values, spectra are not affected by the difference of spin-spin coupling constants.



Figure 4. (a) The <sup>1</sup>H broad band decoupled <sup>13</sup>C NMR spectrum. <sup>13</sup>C PENDANT NMR spectra obtained for (b)  $d_3=3/(8J)$  and (c)  $d_3=(5/(8J)$ .

## 4. Conclusion

One can perform PENDANT NMR experiment for  $d_3 = 3/(8J)$  and 5/(8J). For both values quaternary carbons give negative signals. For  $d_3 = 3/(8J)$ , while CH<sub>2</sub> groups are giving positive signals, CH and CH<sub>3</sub> groups give negative signals. For  $d_3 = 5/(8J)$ , CH<sub>2</sub> groups give negative signals, CH and CH<sub>3</sub> groups give positive signals. For each  $d_3$  value the signs of CH and CH<sub>3</sub> groups signals are the same but CH and CH<sub>3</sub> groups can be identified from each other by looking at their chemical shifts. As a result <sup>13</sup>C PENDANT NMR spectroscopy can be used for identification of C, CH, CH<sub>2</sub> and CH<sub>3</sub> groups.

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## References

- [1] J. Homor and M. C. Perry, J. Chem. Soc. Chem. Commun., (1994), 373.
- [2] J. Homor and M. C. Perry, J. Chem. Soc. Perkin Trans., 2, (1995), 533.

- [3] O. W. Sørensen, G. W. Eich, M. H. Levitt, G. Bodenhausen and R.R. Ernst, Prog. NMR Spectrosc., 16, (1983), 163.
- [4] A. Gençten, Ö. Tezel and A. Köroğlu, Appl. Magn. Reson., 20, (2001), 265.
- [5] I. S. Podkorytov, Concepts Magn. Reson., 9, (1997), 117.
- [6] R. R. Ernst, G. Bodenhausen and A.Wokaun, Principles of Nuclear Magnetic Resonance in One and Two Dimensions, Clarendon Press, Oxford, 1987.
- [7] N. Chandrakumar and S. Subramanian, Modern Techniques in High Resolution FT NMR, Springer, New York, 1987.
- [8] P. J. Hore, J. A. Jones and S. Wimperis, NMR: The Toolkit, Oxford University Press, New York, 2000.
- [9] S. Braun, H. O. Kalinowski and S. Berger, 150 and More Basic NMR Experiments, Wiley-VCH, Weinheim, 1998.