

# Transport property measurements of $\text{Bi}_2\text{Se}_3$ crystal grown by Bridgman method

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Received 14.11.2008

## Abstract

This paper deals with the growth of  $\text{Bi}_2\text{Se}_3$  crystal by newly designed experimental set-up of Bridgman technique in our laboratory. Grown crystal is characterized by EDAX (Energy Dispersive Analysis of X-rays), XRD (X-ray Diffraction), low temperature thermopower measurements (17–284 K), resistivity measurements (16–294 K) and Hall Effect at room temperature in order to study its various properties. The surface study of the grown crystal using AFM (Atomic Force Microscopy) shows a hexagonal unit cell shape whose internal angle determined comes out to be nearly equal to  $122.94^\circ$  which has close resemblance with an angle of  $120^\circ$  of perfect internal angle of hexagon. Various parameters obtained from above measurements like lattice parameters, crystallite size and stacking fault probabilities are discussed in detail in the paper.

**Key Words:** Crystal growth, transport properties, thermoelectric materials, atomic force microscopy.

**PACS:** 72.15.Eb; 72.15.Jf

## 1. Introduction

$\text{Bi}_2\text{Se}_3$  is a narrow band gap material crystallizing in hexagonal structure [1].  $\text{Bi}_2\text{Se}_3$  has useful application in the field of thermoelectric devices as solid state coolers or generators [2–5] therefore studies on various properties of  $\text{Bi}_2\text{Se}_3$  are interesting for both basic and applied research. Even though bismuth selenide is not as technologically important as bismuth telluride,  $\text{Bi}_2\text{Se}_3$  is properly crystallizable under controlled conditions and easily cleavable. Hence it could be considered a model compound among thermoelectric materials for both experimental and theoretical analysis.

## 2. Experimental

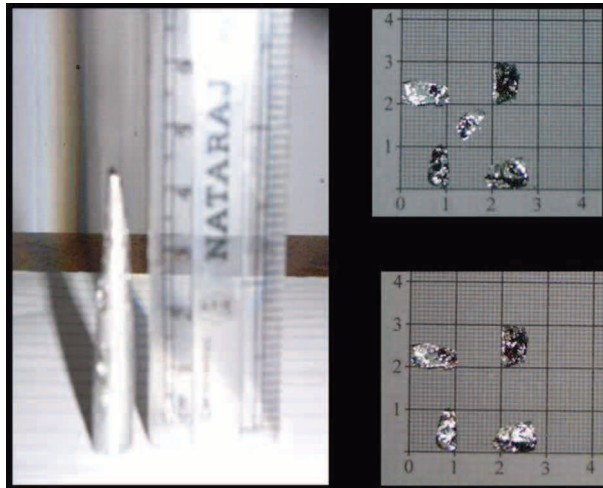
The basic process of crystal growth by Bridgman method is mentioned by Brice [6]. We have designed in our laboratory an experimental set up which implements a slight modification in this technique and is used for the growth of  $\text{Bi}_2\text{Se}_3$  crystal.

Modifications made in the Bridgman set up are: (a) Use of 900 rpm motor with gear box, instead of a stepper motor; (b) Use of threaded shaft and threaded screw, instead of a pulley mechanism for lowering of sample; (c) Use of flip-flop timer circuit for controlling the lowering rate.

Advantages of the modified set up are: (a) Accurate displacement of ampoule; (b) The elastic impact of temperature on sample holder wire is nullified by keeping its length short; (c) The problem of jerks along the linear motion is nullified here; (d) New design of set up is of low cost.

The quartz ampoule containing  $\text{Bi}_2\text{Se}_3$  material is sealed at  $10^{-5}$  torr and placed in a vertical high temperature furnace at a temperature of  $715^\circ\text{C}$  (tip of the ampoule). The lowering rate of this ampoule is kept at  $0.5\text{ mm/hr}$ . A crystal grown by this technique and cleaved portions are shown in Figure 1.

The stoichiometry of the grown crystal is confirmed by EDAX. Further, characterization is done by X-ray diffraction in order to calculate lattice parameters, crystallite size and stacking fault probabilities of this sample. As the material is thermoelectric in nature, we measured the thermopower in the temperature range 17 K to 284 K and Vander Pauw resistivity in the temperature range 16 K to 294 K with existing facilities available at IUC-DAE Indore. Hall effect measurements were done at room temperature on this sample via a Lakeshore 7504 Hall measurement system in our department. To gain insight into the surface of the cleaved crystals, analysis using a atomic force microscope was also carried out.

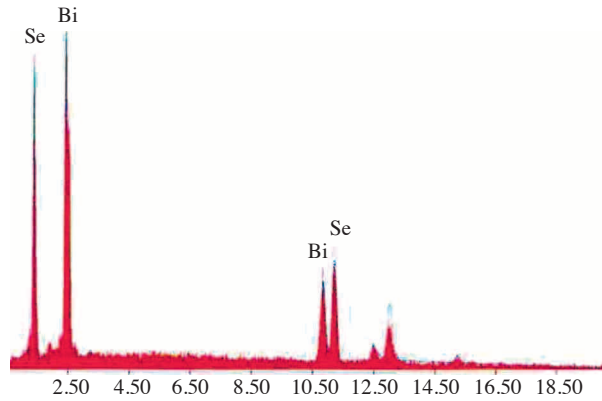


**Figure 1.** Photograph of as-grown and cleaved crystal of  $\text{Bi}_2\text{Se}_3$ .

### 3. Results and discussion

#### 3.1. Energy Dispersive Analysis of X-rays

The EDAX spectra shown in Figure 2 of the sample shows that the grown crystal is free from any other impurities; and Table 1 provides the mass fraction of each element, i.e. bismuth and selenium, used during the growth as well that measured via EDAX. This indicates the stoichiometry in the crystal is well maintained.



**Figure 2.** EDAX spectra of  $\text{Bi}_2\text{Se}_3$  crystal.

**Table 1.** Results obtained from EDAX.

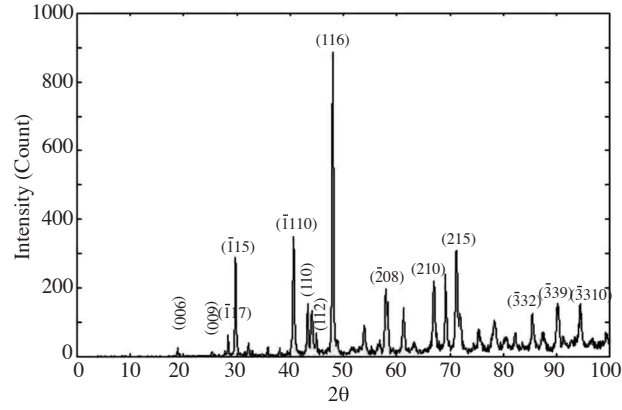
Element	Growth as mixed, wt%	EDAX, wt%
Bi	63.80	61.73
Se	36.20	38.27

#### 3.2. X-ray diffraction

X-ray diffractogram of powder  $\text{Bi}_2\text{Se}_3$  was obtained using a Philips X-ray diffractometer and is shown in Figure 3. The values of lattice parameters, X-ray density and volume, are calculated for this sample and shown in Table 2; the values have close resemblance with reported values. Calculations of crystallite size were carried out using the Scherrer formula [7]:

$$t = \frac{k\lambda}{\beta_{2\theta} \cos \theta}, \quad (1)$$

where  $k$  is constant having value 0.9,  $\lambda$  is the wavelength of the X-ray source,  $\beta_{2\theta}$  is the FWHM (full width at half maximum) line width of the intensity lines. Calculated crystallite size shows variation from 116 Å to 695 Å for different reflections taken into consideration.



**Figure 3.** X-ray diffractogram of  $\text{Bi}_2\text{Se}_3$  compound.

**Table 2.** Lattice Parameters, unit cell volume and X-ray density obtained from X-ray diffractogram of  $\text{Bi}_2\text{Se}_3$  sample.

Parameter	$\text{Bi}_2\text{Se}_3$	
	Reported [8]	Calculated
a (Å)	4.13	4.12
c (Å)	28.62	28.63
c/a ratio	6.92	6.94
Volume $V=(\sqrt{3}/2)a^2c \text{ \AA}^3$	425.14	422.18
X-ray density (gm/cc)	7.676	7.720

Warren and Agarwal et al. [9, 10] has shown that, in the case of hexagonal closed-packed structure, it is possible to make a realistic estimation of both the deformation fault probabilities  $\alpha$  and growth fault probability  $\beta$  by measuring the half width of the X-ray diffraction lines using the following expression:

$$\text{For even } l : (3\alpha + 3\beta) = \frac{B_{2\theta}\pi^2 c^2}{360 l d^2 \tan \theta} \quad (2)$$

$$\text{For odd } l : (3\alpha + \beta) = \frac{B_{2\theta}\pi^2 c^2}{360 l d^2 \tan \theta}, \quad (3)$$

where  $B_{2\theta}$  is the full line width, expressed in degrees, at half the maximum intensity,  $c = 2d_{002}$ ,  $l$  is a Miller index,  $d$  is the interplanar spacing for the reflection,  $\alpha$  is deformation fault probability and  $\beta$  is the growth fault probability.

Deformation fault probability  $\alpha$  and growth fault probability  $\beta$ , calculated from the above equations, are shown in Table 3, and the values indicate that there may be a deformation fault probability of 23 per 1000 atomic layers, and growth fault probability of 10 per 1000 atomic layers for  $\text{Bi}_2\text{Se}_3$  samples.

**Table 3.** Deformation fault probability  $\alpha$  and growth fault probability  $\beta$  for  $\text{Bi}_2\text{Se}_3$  crystal.

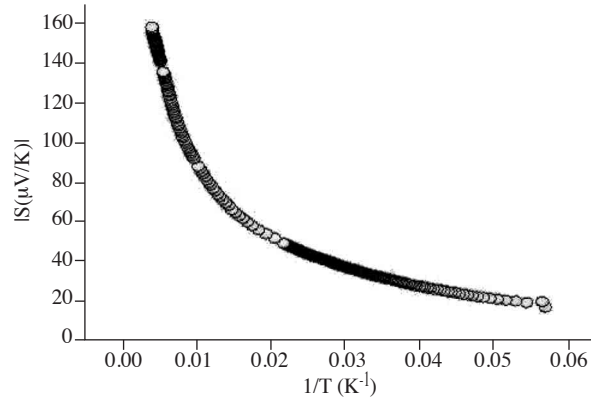
Reflections	$(\bar{3}38), (\bar{3}39)$
$\beta_{2\theta}$ (Degree)	0.24, 0.36
$3\alpha + 3\beta$	0.06
$3\alpha + \beta$	0.08
$\alpha$	0.023
$\beta$	0.010

The values of  $\alpha$  shown in Table 3 clearly indicate that a high density of deformation faults were introduced into the specimen and the actual number depended upon the amount of deformation introduced into the sample during experiment. In the case of growth fault probability, a firm conclusion is difficult in view of small values of  $\beta$ . But, it is presumed that stacking faults may be responsible for the conductivity phenomena in this sample.

### 3.3. Low temperature Thermoelectric Power (TEP) measurement

As  $\text{Bi}_2\text{Se}_3$  is known to be a good thermoelectric material, it is essential to measure its thermoelectric power  $S$  in order to calculate its figure of merit. Hence, Figure 4 shows the variation of Seebeck coefficient with an inverse of temperature for  $\text{Bi}_2\text{Se}_3$  crystal in the temperature range 16 K to 200 K.

A study from Figure 4 reveals that in all the cases, the absolute value of  $S$  increases steadily with an increase in temperature, for  $\text{Bi}_2\text{Se}_3$  sample, such increase of  $S$  at lower temperature is due to the decrease of electron mobility with temperature [11, 12]. Secondly the sign of TEP depends on whether the majority carriers are electrons or holes. The fact that TEP in  $\text{Bi}_2\text{Se}_3$  crystal is negative clearly indicates that this crystal is n-type in nature.

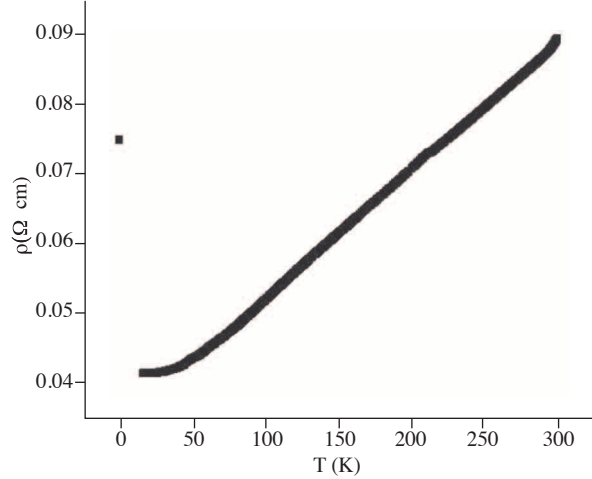
**Figure 4.** Plot of thermoelectric power  $S$  as a function of inverse of temperature for  $\text{Bi}_2\text{Se}_3$  crystal.

### 3.4. Low temperature resistivity measurements

The set-up to conduct resistivity measurement is similar to that used for Seebeck coefficient measurement except the way contacts were established on the sample. In the present Seebeck measurement, we use two copper block sample holders and the sample is placed in between these two blocks; in case of resistivity measurement,

four contacts were made onto the sample with copper wires and current was allowed to pass through two outer contacts and voltage is measured between the two inner contacts.

Figure 5 shows how  $\text{Bi}_2\text{Se}_3$  crystal resistivity varies in the temperature range 16–294 K. The peculiar result, seen in Figure 5, is that resistivity goes on increasing with temperature, i.e. electrical conductivity monotonically decreases with temperature and matches with the result observed by [11–19].



**Figure 5.** Plot of resistivity  $\rho$  as function of temperature  $T$  in  $\text{Bi}_2\text{Se}_3$  crystal.

As explained in [12], for values measured above 300 K, resistivity decreases with increase in temperature. However, high temperature resistivity measurements were not possible due to the experimental setup in this investigation. It is clear such crystals can exhibit semimetallic conduction up to 300 K above which they can show semiconducting behavior, and from where we can obtain the transition temperature. The semimetallic character arises in  $\text{Bi}_2\text{Se}_3$  due to the half filled 6p band overlapping the filled 6s band. It is also stated [12] the presence of interstitial defects may result in ionized states with rise in temperature and provide free electrons for the conduction mechanism, thereby decreasing the absolute value of the electrical resistivity.

In [11] is reported that, in low temperature portion of the resistivity measurements, semiconducting behavior can be observed based on the purity of material used. In our case, increase of electrical resistivity with temperature in the low temperature region can be attributed to the temperature dependence of carrier mobility [18].

### 3.5. Hall Effect Measurements

In order to support the present results, Hall effect measurements on  $\text{Bi}_2\text{Se}_3$  crystal has been carried out at room temperature using a Lakeshore 7504 Hall measurement system [20]. The measurements were carried out by passing a 100  $\mu\text{A}$  current through the sample under magnetic fields +5 kG to -5 kG; data is shown in Table 4. The results obtained show that all the Hall coefficients,  $R_H$ , are negative, which means that our sample is n-type in nature thereby supporting the Seebeck coefficient measurements. Values of  $R_H$  obtained varies from -1.6 to -3.3  $\text{cm}^3/\text{C}$  and are somewhat higher than reported [12, 21]; mobility  $\mu_H$  varies from  $4.68 \times 10^2$  to  $1.15 \times 10^3$ , which are also higher than reported [22]; and carrier density  $n$  varies from  $0.5 \times 10^{18}$  to  $3.6 \times 10^{18}$

$\text{cm}^{-3}$ , which is one power lower than the reported values [12, 22, 23]. The measured zero field resistivity comes out to be  $86 \text{ m}\Omega \cdot \text{cm}$ ; whereas the reported values are 3 to  $4 \text{ m}\Omega \cdot \text{cm}$ .

**Table 4.** Values of Hall coefficient  $R_H$ , mobility  $\mu_H$ , carrier concentration  $n$  of  $\text{Bi}_2\text{Se}_3$  crystal. Current =  $100 \mu\text{A}$ ; Zero field Resistivity =  $8.623 \times 10^{-2} \Omega \cdot \text{cm}$ .

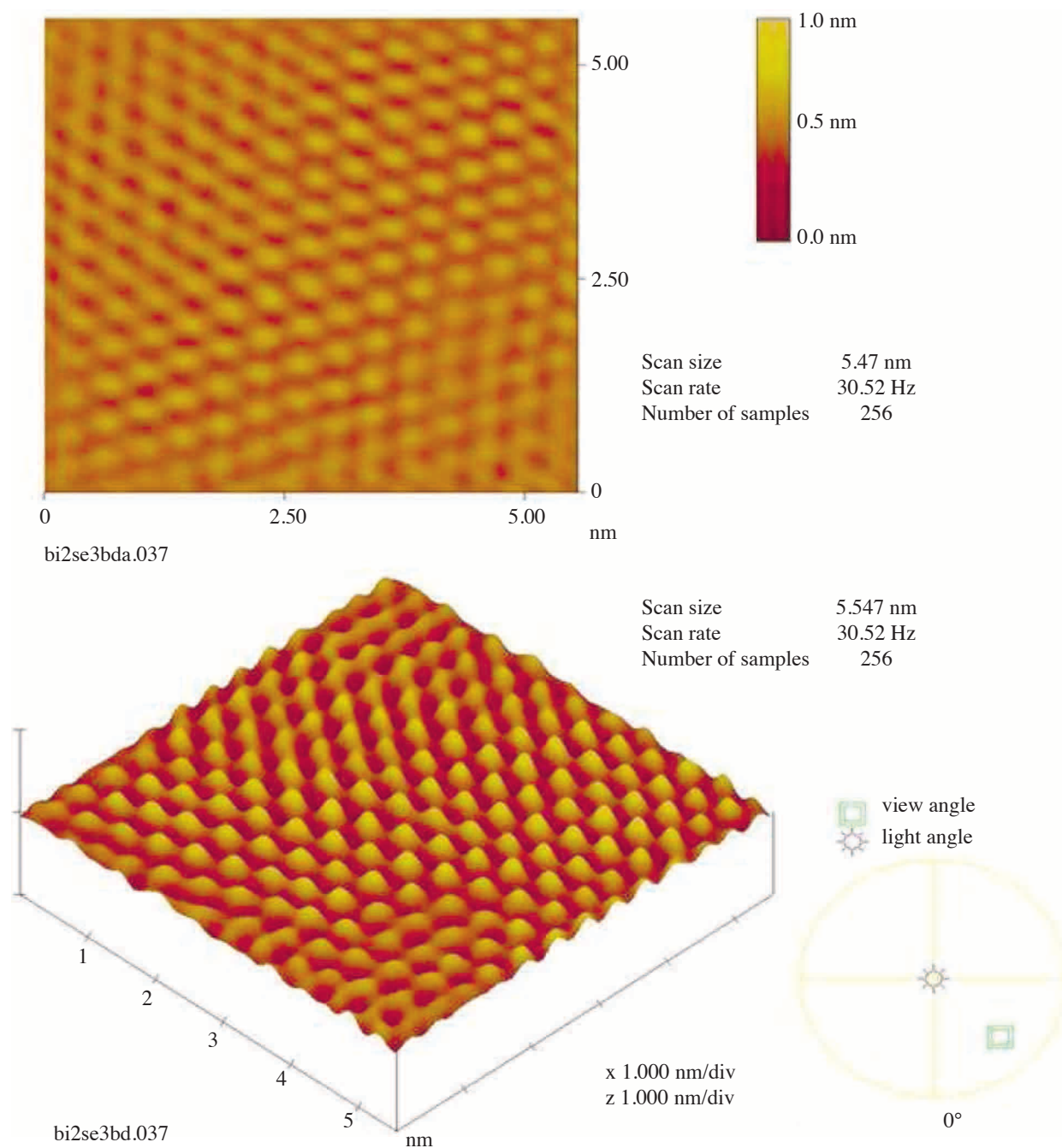
$B$ (kG)	Hall coefficient, $R_H$ ( $\text{cm}^3/\text{C}$ )	Hall Mobility, $\mu_H$ ( $\text{cm}^2/\text{Vs}$ )	Density, $n$ ( $\text{cm}^{-3}$ )
+5	-2.246	$6.2 \times 10^2$	$2.7 \times 10^{18}$
+4	-4.177	$1.1 \times 10^3$	$1.4 \times 10^{18}$
+3	-3.065	$8.4 \times 10^2$	$2.0 \times 10^{18}$
+2	-1.697	$4.6 \times 10^2$	$3.6 \times 10^{18}$
+1	-3.365	$9.2 \times 10^2$	$1.8 \times 10^{18}$
-1	-11.39	$3.1 \times 10^3$	$5.4 \times 10^{17}$
-2	-2.357	$6.5 \times 10^2$	$2.6 \times 10^{18}$
-3	-3.898	$1.0 \times 10^3$	$1.6 \times 10^{18}$
-4	-4.317	$1.1 \times 10^3$	$1.4 \times 10^{18}$
-5	-2.547	$7.0 \times 10^2$	$2.4 \times 10^{18}$

### 3.6. Atomic Force Microscopy (AFM) surface studies

The as-grown crystal of  $\text{Bi}_2\text{Se}_3$  was viewed under contact mode with a Veeco AFM and a silicon nitride tip was used to obtain a topographic image of the sample surface. The Fourier transform images obtained with the help of the Nanoscope Controller software for Veeco scanning force microscopes is displayed in Figure 6; the images show 2-D and 3-D topographic images of the crystal surface thereby confirming the regular (periodic) arrangement of atoms throughout the ( $5.547 \text{ nm square}$ ) scanned region of the sample.

Figure 7 shows the section analysis for the periodicity exhibited in Figure 6. The analysis makes clear the atomic arrangement is periodic. The inset values shows the horizontal distance between two successive atoms and are nearly equal to  $4.14 \text{ \AA}$  on both a and b axes. Figure 8 shows the section analysis for angle, of Fourier transform image of Figure 6 representing a hexagonal unit cell shape whose angle determined comes out to be nearly equal to  $122.94^\circ$  and has close resemblance to the  $120^\circ$  of a perfect hexagon.

$\text{Bi}_2\text{Se}_3$  crystal has been grown successfully in our laboratory using the modified Bridgman technique. Seebeck co-efficient and Hall effect measurements indicates that the sample is n-type conductive in nature. The increase in resistivity from low temperature to  $300 \text{ K}$  is attributed to the semi-metallic behavior of this crystal. Atomic Force Microscope images reveals the regular arrangements of atoms in the  $5.547 \text{ nm}$  scanned region and also provides a measure of the hexagonal unit cell angle which nearly equals to  $122.94^\circ$ .



**Figure 6.** 2-D, 3-D Fourier transform images of  $\text{Bi}_2\text{Se}_3$  crystal.



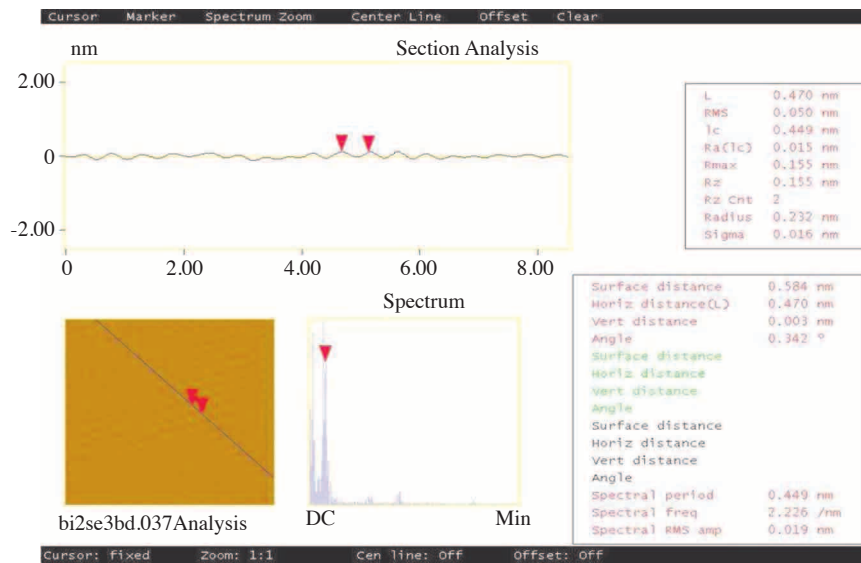


Figure 7. Section analysis (periodicity) of Fourier transform image taken at atomic scale.

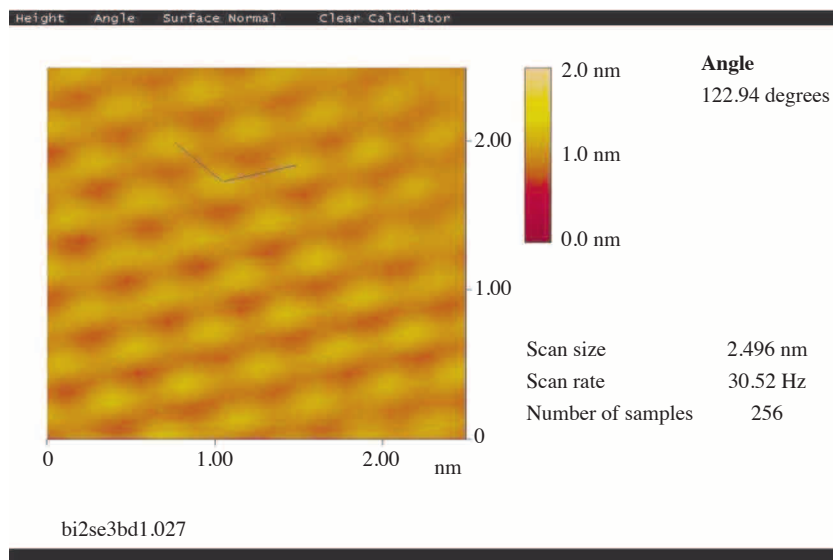


Figure 8. Section analysis (angle) showing internal angle of hexagonal unit cell.

## Acknowledgements

Authors are thankful to UGC for providing DRS/SAP (III<sup>rd</sup> phase) programme to the Department of Physics, Sardar Patel University, which has made this work possible. Thanks are specifically directed to Dr. V. Ganesan, Miss Swati Pandya and other students of the low temperature laboratory IUC-DAE, Indore for helping round the clock to carry out TEP, Low temperature resistivity and AFM work.

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